

Periodic task scheduling

An exact test for EDF

Relative deadlines less than periods

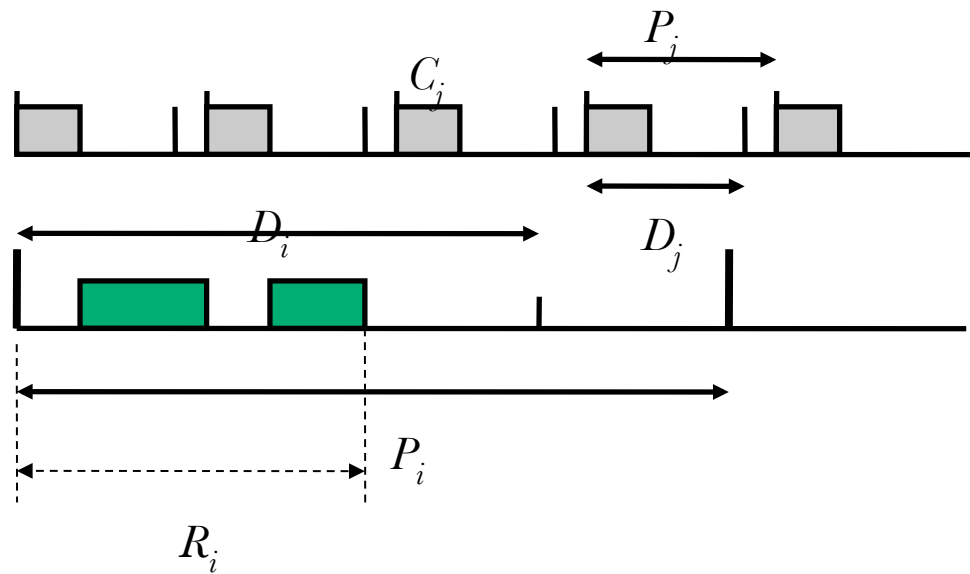
Processor demand criterion

The earliest deadline first policy

- Optimal scheduling policy when relative deadlines are equal to task periods
- Is a dynamic priority policy
- How does it behave when relative deadlines are less than periods?
- Exact analysis for EDF

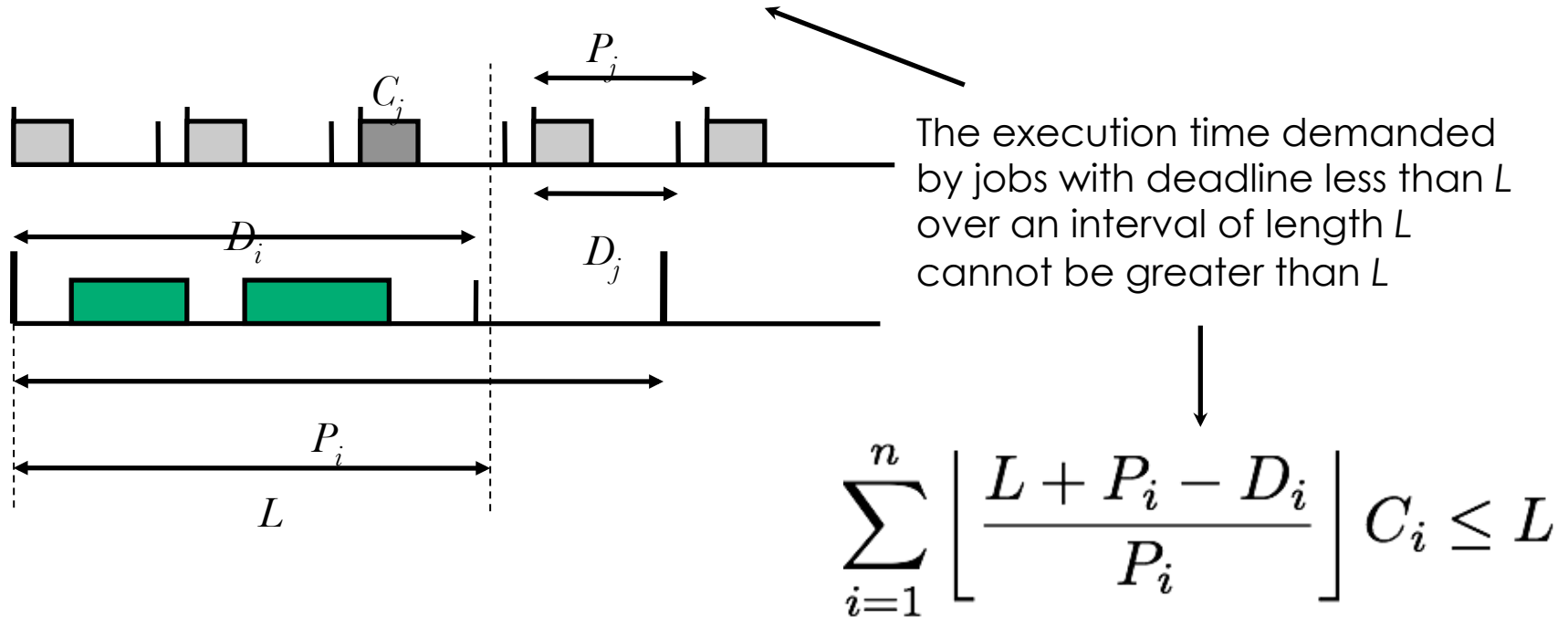
EDF and processor demand

- Interference is due to only those tasks with earlier deadlines



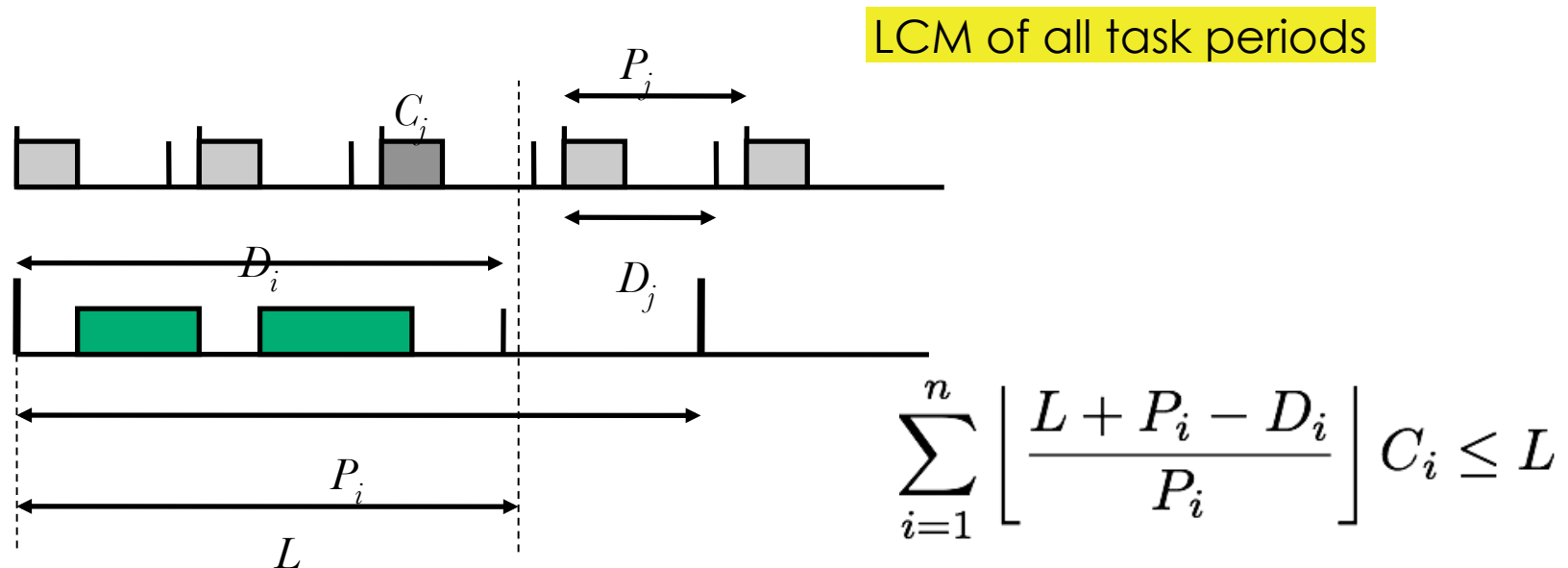
EDF and processor demand

- Consider demand on the processor due to tasks whose deadlines have passed
- Within any time interval, L , the demand must be less than L .



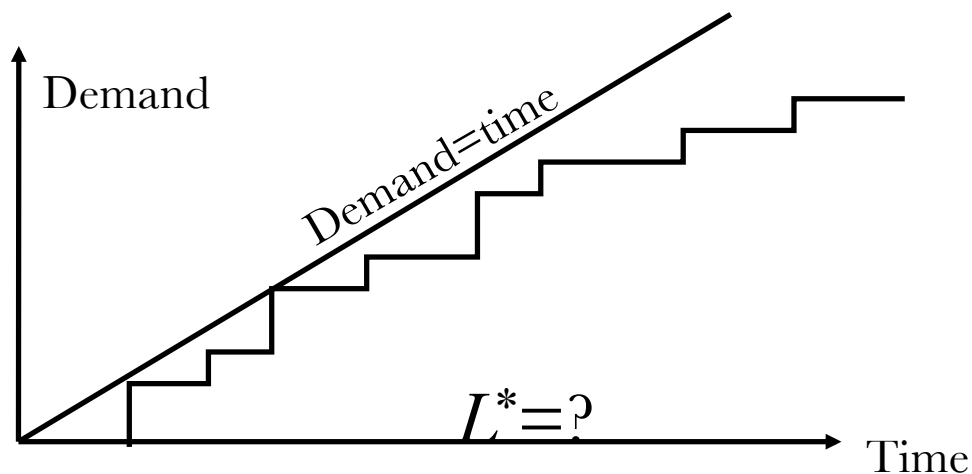
Processor demand

- Checking the schedulability for at all time instants is not possible
 - Overwhelming complexity
- Observation 1: Sufficient to check up to the hyperperiod (schedule repeats itself)
- Observation 2: Check only at absolute deadlines



Processor demand

- Checking the schedulability for at all time instants is not possible
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- Observation 1: Sufficient to check up to the hyperperiod (schedule repeats itself)
- Observation 2: Check only at absolute deadlines
- Observation 3: If $U < 1$, the demand is trivially satisfied after some time instant L^*



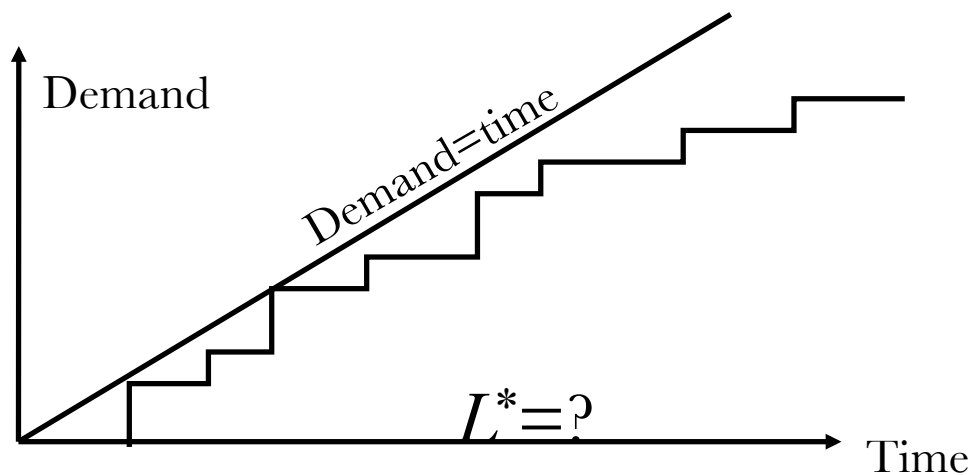
$$\sum_{i=1}^n \left\lceil \frac{L + P_i - D_i}{P_i} \right\rceil C_i \leq L$$

Processor demand

- Deriving L^*

$$\sum_{i=1}^n \left\lfloor \frac{L + P_i - D_i}{P_i} \right\rfloor C_i \leq L$$

$$\sum_{i=1}^n \left\lfloor \frac{t + P_i - D_i}{P_i} \right\rfloor C_i \leq \sum_{i=1}^n \frac{t - D_i + P_i}{P_i} C_i = tU + \sum_{i=1}^n (P_i - D_i)U_i$$

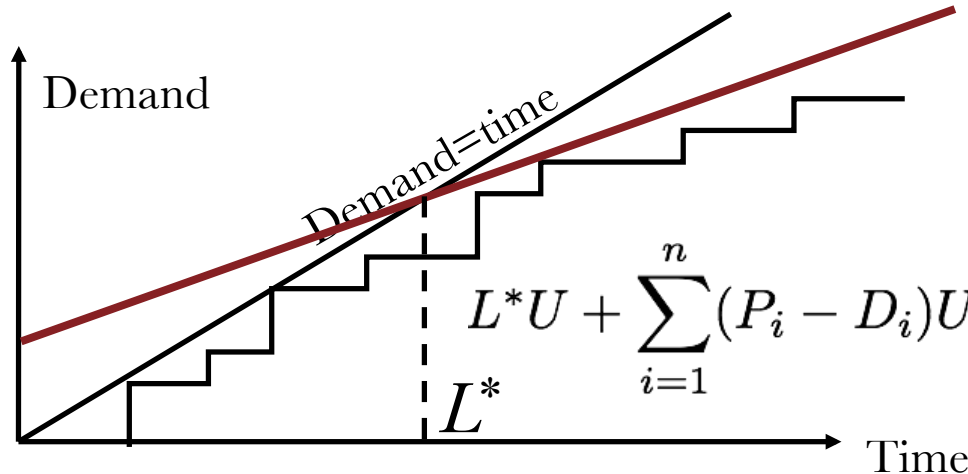


Processor demand

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$$\sum_{i=1}^n \left\lfloor \frac{L + P_i - D_i}{P_i} \right\rfloor C_i \leq L$$

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$$L^*U + \sum_{i=1}^n (P_i - D_i)U_i = L^* \Rightarrow L^* = \frac{\sum_{i=1}^n (P_i - D_i)U_i}{1 - U}$$

Processor demand criterion

- Check if
$$\sum_{i=1}^n \left\lfloor \frac{L + P_i - D_i}{P_i} \right\rfloor C_i \leq L$$

- for all L that are absolute deadlines in the interval $[0, L^*]$

- where

$$L^* = \frac{\sum_{i=1}^n (P_i - D_i) U_i}{1 - U}$$

- This is an exact test for EDF when relative deadlines are less than task periods

Example using processor demand

- Consider the following task set

- $T_1: (C_1=1, P_1=3, D_1=2)$
- $T_2: (C_2=2, P_2=7, D_2=5.5)$
- $T_3: (C_3=2, P_3=10, D_3=6)$

- The task set has a hyperperiod of 210

- However, we only need to test deadlines up to $L^* = \frac{\sum_{i=1}^n (P_i - D_i) U_i}{1 - U}$

- $U = 86/105 = 0.8190$; $L^* = 8.63$

- At $L=2$:

$$\lfloor \frac{L + P_1 - D_1}{P_1} \rfloor C_1 = \lfloor \frac{2 + 3 - 2}{3} \rfloor 1 = 1$$

Example using processor demand

- Consider the following task set

- $T_1: (C_1=1, P_1=3, D_1=2)$
- $T_2: (C_2=2, P_2=7, D_2=5.5)$
- $T_3: (C_3=2, P_3=10, D_3=6)$

- The task set has a hyperperiod of 210

- However, we only need to test deadlines up to $L^* = \frac{\sum_{i=1}^n (P_i - D_i) U_i}{1 - U}$

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- At $L=5.5$: (also need to check at $L=5$; not shown here)

$$\lfloor \frac{L + P_1 - D_1}{P_1} \rfloor C_1 + \lfloor \frac{L + P_2 - D_2}{P_2} \rfloor C_2 = \lfloor \frac{5.5 + 3 - 2}{3} \rfloor 1 + \lfloor \frac{5.5 + 7 - 5.5}{7} \rfloor 2 = 2 + 2 = 4$$

Example using processor demand

- Consider the following task set

- $T_1: (C_1=1, P_1=3, D_1=2)$
- $T_2: (C_2=2, P_2=7, D_2=5.5)$
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- At $L=6$:

$$\lfloor \frac{6 + 3 - 2}{3} \rfloor 1 + \lfloor \frac{6 + 7 - 5.5}{7} \rfloor 2 + \lfloor \frac{6 + 10 - 6}{10} \rfloor 2 = 6$$

Example using processor demand

- Consider the following task set

- $T_1: (C_1=1, P_1=3, D_1=2)$
- $T_2: (C_2=2, P_2=7, D_2=5.5)$
- $T_3: (C_3=2, P_3=10, D_3=6)$

- The task set has a hyperperiod of 210

- However, we only need to test deadlines up to $L^* = \frac{\sum_{i=1}^n (P_i - D_i) U_i}{1 - U}$

- $U = 86/105 = 0.8190$; $L^* = 8.63$

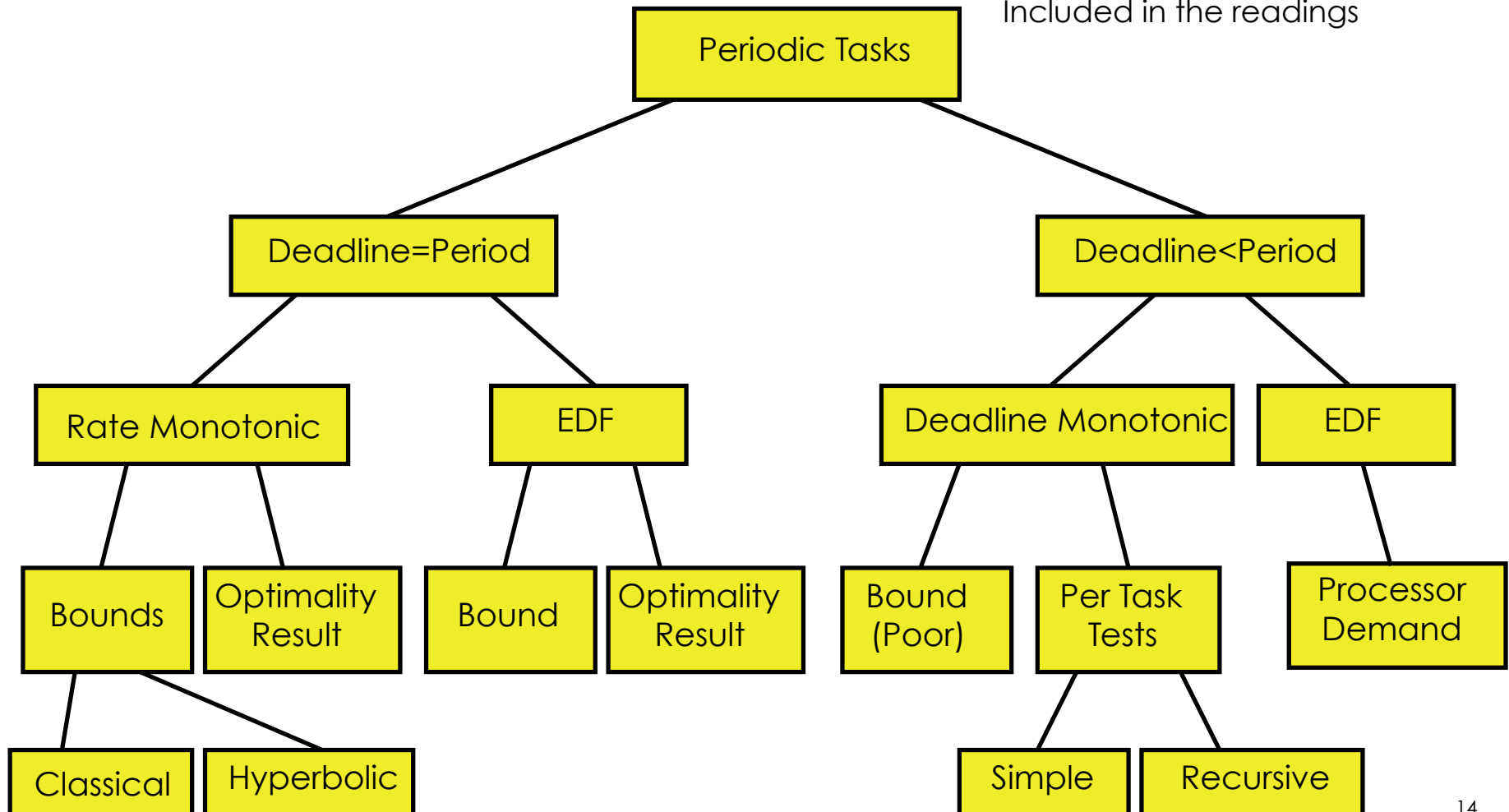
- At $L=8$:

$$\lfloor \frac{8+3-2}{3} \rfloor 1 + \lfloor \frac{8+7-5.5}{7} \rfloor 2 + \lfloor \frac{8+10-6}{10} \rfloor 2 = 3 + 2 + 2 = 7$$

No more absolute deadlines < 8.63 . We are done!

Topics covered so far

Chapter 4 of Buttazzo's text
Included in the readings



Lecture summary

- Exact test for EDF scheduling (relative deadlines $<$ periods)
- Processor demand criterion