

# Key Establishment

EECE 412

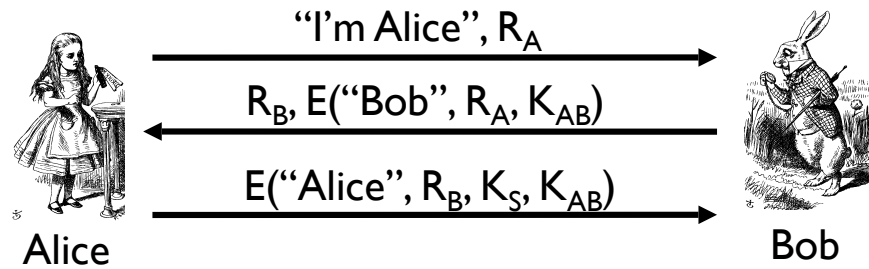
“The security of a cryptosystem must not depend on keeping secret the crypto-algorithm. The security depends only on keeping secret the key”

Auguste Kerckhoff von Nieuwenhof

Dutch linguist

1883

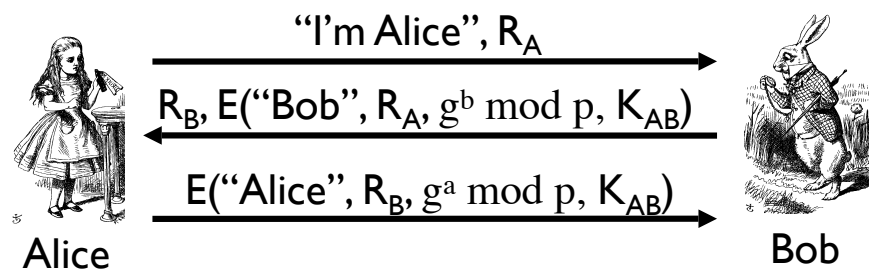
# session key with mutual authentication using symmetric key



Tuesday, September 25, 2007

3

# FPS session key with mutual authentication using symmetric key



Tuesday, September 25, 2007

4

# Outline

1. Diffie-Hellman key exchange (4.4)
2. mutual authentication in networks (9.1-9.3.3)
3. perfect forward secrecy (9.3.4, 9.3.5)

# Notation

- $X \rightarrow Y : \{ Z \parallel W \}_{k_{X,Y}}$ 
  - X sends Y the message produced by concatenating Z and W enciphered by key  $k_{X,Y}$ , which is shared by users X and Y
- $A \rightarrow T : \{ Z \}_{k_A} \parallel \{ W \}_{k_{A,T}}$ 
  - A sends T a message consisting of the concatenation of Z enciphered using  $k_A$ , A's key, and W enciphered using  $k_{A,T}$ , the key shared by A and T
- $r_1, r_2$  nonces (“nonrepeating” random numbers)

# Diffie-Hellman Key Exchange

Tuesday, September 25, 2007

7

## important trivia

- Invented by Williamson (GCHQ) and, independently, by D and H (Stanford)
- A “key exchange” algorithm
  - Used to establish a shared symmetric key
- Not for encrypting or signing
- Security rests on difficulty of **discrete log** problem:  
given  $g$ ,  $p$ , and  $g^k \bmod p$  find  $k$

Tuesday, September 25, 2007

8

# how it works

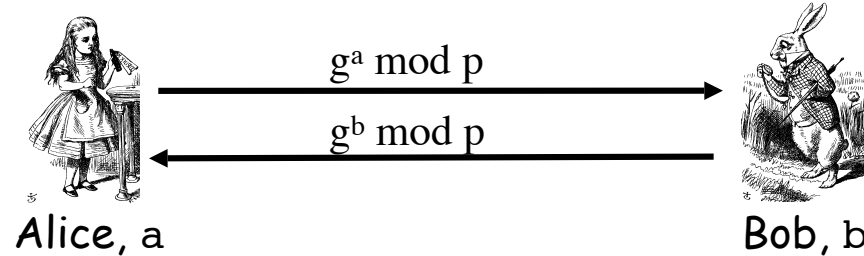
- Let  $p$  be prime, let  $g$  be a **generator**
  - For any  $x \in \{1, 2, \dots, p-1\}$  there is  $n$  s.t.  $x = g^n \pmod p$
- 1. Alice selects secret value  $a$
- 2. Bob selects secret value  $b$
- 3. Alice sends  $g^a \pmod p$  to Bob
- 4. Bob sends  $g^b \pmod p$  to Alice
- 5. Both compute shared secret  $g^{ab} \pmod p$ 
  - Shared secret can be used as symmetric key

# why it's hard to attack

- Suppose that Bob and Alice use  $g^{ab} \pmod p$  as a symmetric key
- Trudy can see  $g^a \pmod p$  and  $g^b \pmod p$
- Note  $g^a g^b \pmod p = g^{a+b} \pmod p \neq g^{ab} \pmod p$
- If Trudy can find  $a$  or  $b$ , system is broken
- If Trudy can solve **discrete log** problem, then she can find  $a$  or  $b$

# the protocol

- **Public:**  $g$  and  $p$
- **Secret:** Alice's exponent  $a$ , Bob's exponent  $b$

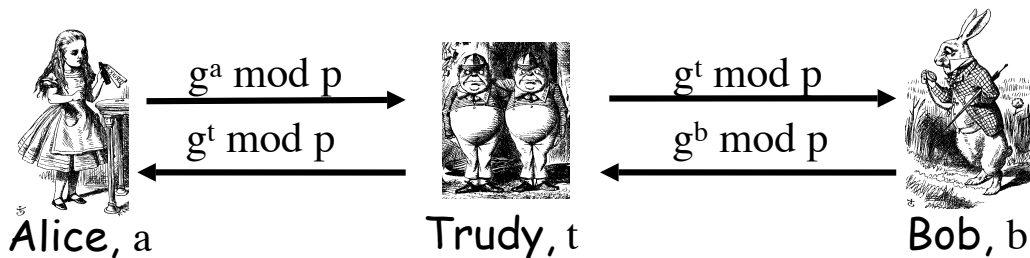


- Alice computes  $(g^b)^a = g^{ba} = g^{ab} \bmod p$
- Bob computes  $(g^a)^b = g^{ab} \bmod p$
- Could use  $K = g^{ab} \bmod p$  as symmetric key

Tuesday, September 25, 2007

11

# Man-in-the-Middle Attack



- Trudy shares secret  $g^{at} \bmod p$  with Alice
- Trudy shares secret  $g^{bt} \bmod p$  with Bob
- Alice and Bob don't know Trudy exists!

Tuesday, September 25, 2007

12

# how to prevent MiM attack?

- Encrypt DH exchange with symmetric key
- Encrypt DH exchange with public key
- Sign DH values with private key
- Other?

You **MUST** be aware of MiM attack on Diffie-Hellman

# Authentication Protocols

# basics

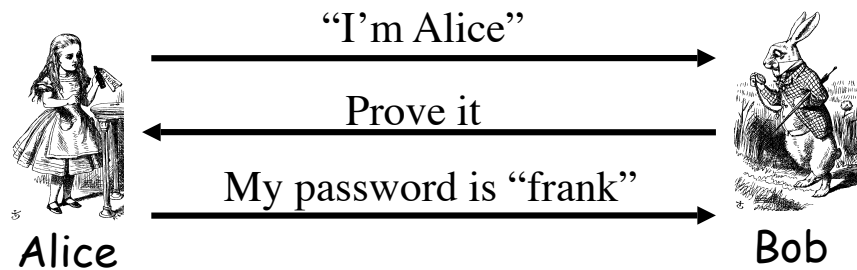
- Alice must prove her identity to Bob
  - Alice and Bob can be humans or computers
- May also require Bob to prove he's Bob (mutual authentication)
- May also need to establish a session key
- May have other requirements, such as
  - Use only public keys
  - Use only symmetric keys
  - Use only a hash function
  - Anonymity, plausible deniability, etc., etc.

# why authentication can be hard?

- relatively simple on a stand-alone computer
  - “Secure path” is the primary issue
  - main concern is an attack on authentication software
- much more complex over a network
  - attacker can passively observe messages
  - attacker can replay messages
  - active attacks may be possible (insert, delete, change messages)

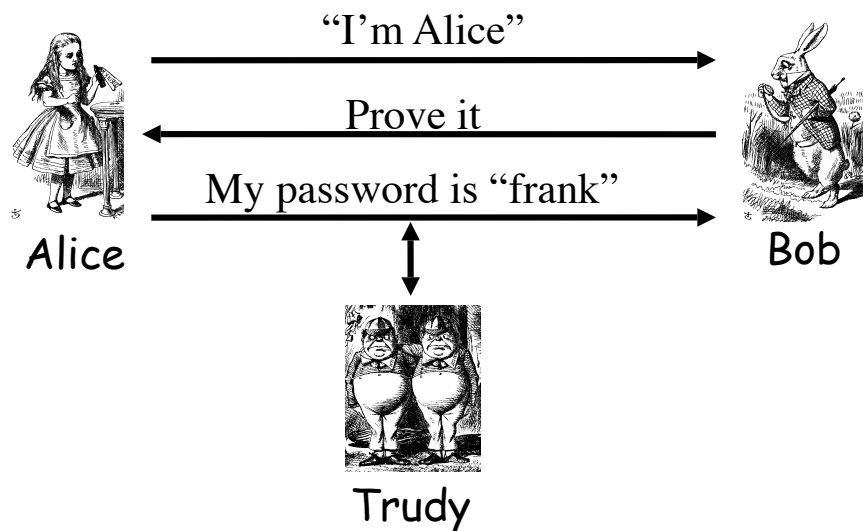


# simple authentication

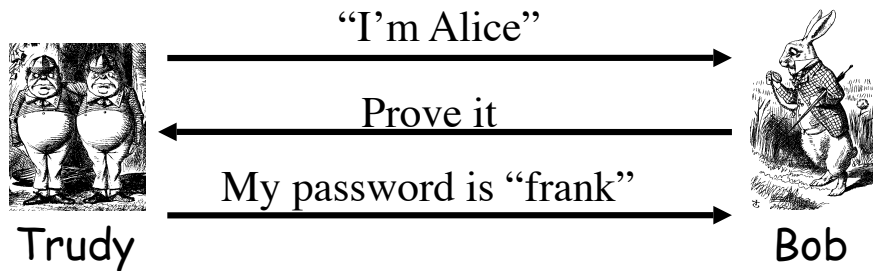


- Simple and may be OK for standalone system
- But insecure for networked system
  - Subject to a replay attack (next 2 slides)
  - Bob must know Alice's password

# authentication attack

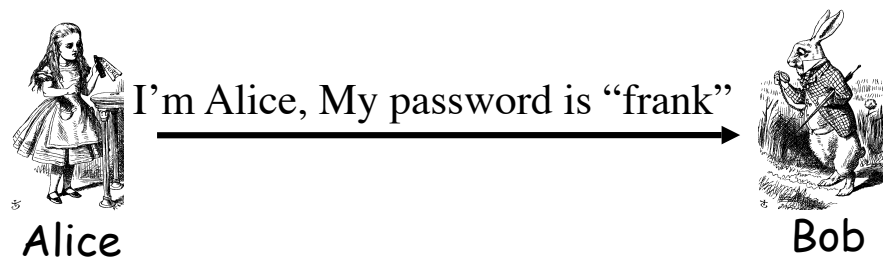


# Authentication Attack



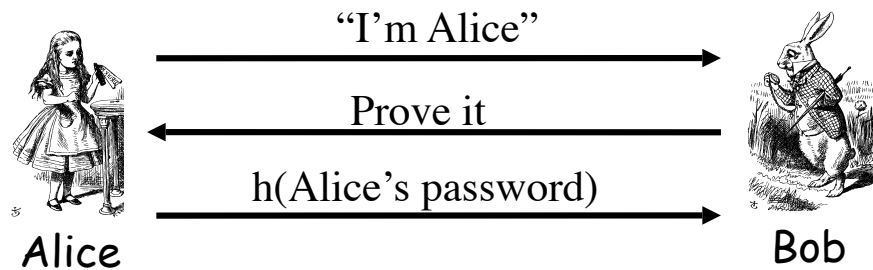
- This is a **replay** attack
- How can we prevent a replay?

# Simple Authentication



- More efficient...
- But same problem as previous version

# Better Authentication

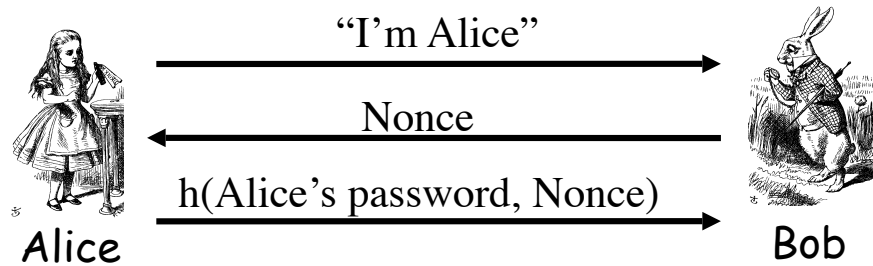


- Better since it hides Alice's password
  - From both Bob and attackers
- But still subject to replay

# challenge-response

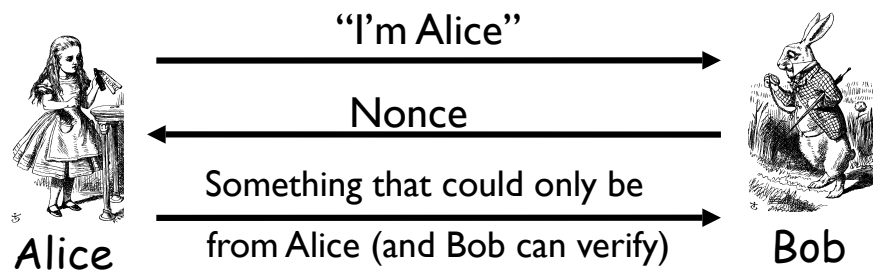
- To prevent replay, challenge-response used
- Suppose Bob wants to authenticate Alice
  - Challenge sent from Bob to Alice
  - Only Alice can provide the correct response
  - Challenge chosen so that replay is not possible
- How to accomplish this?
  - Password is something only Alice should know...

# simple challenge-response



- Nonce is the **challenge**
- The hash is the **response**
- Nonce prevents replay, insures freshness
- Password is something Alice knows
- Note that Bob must know Alice's password

# general challenge-response



- What can we use to achieve this?
- Hashed pwd works, crypto might be better

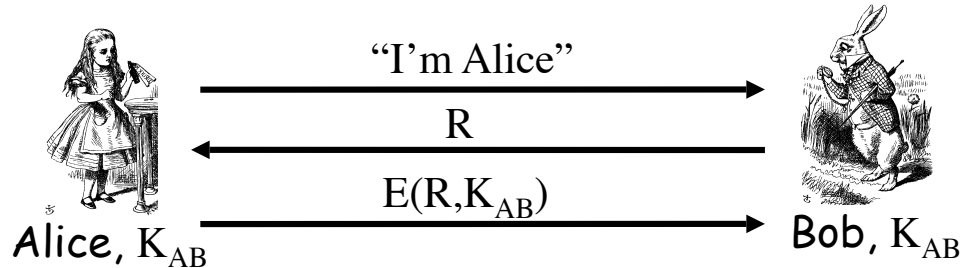
# symmetric key notation

- Encrypt plaintext  $P$  with key  $K$   
 $C = E(P,K)$
- Decrypt ciphertext  $C$  with key  $K$   
 $P = D(C,K)$
- Here, we are concerned with attacks on **protocols**, not directly on the crypto
- We assume that crypto algorithm is secure

# authentication with symmetric key

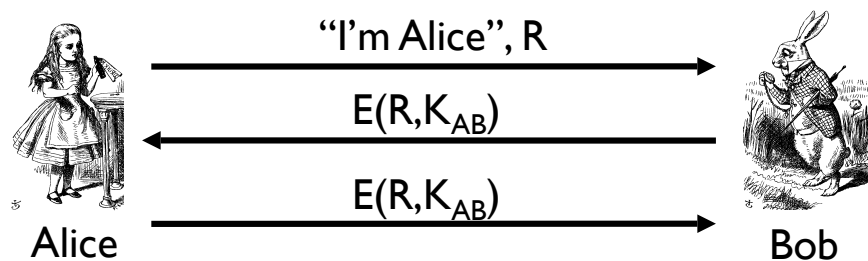
- Alice and Bob share symmetric key  $K_{AB}$
- key  $K_{AB}$  known only to Alice and Bob
- authenticate by proving knowledge of shared symmetric key
- how to accomplish this?
  - must not reveal key
  - must not allow replay attack

# authentication with symmetric key



- Secure method for Bob to authenticate Alice
- Alice does not authenticate Bob
- Can we achieve mutual authentication?

# mutual authentication?



- What's wrong with this picture?
- "Alice" could be Trudy (or anybody else)!

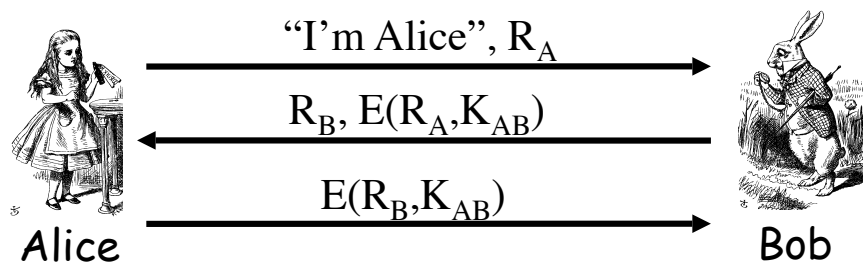
# Mutual Authentication

- Since we have a secure one-way authentication protocol...
- The obvious thing to do is to use the protocol twice
  - Once for Bob to authenticate Alice
  - Once for Alice to authenticate Bob
- This has to work...

Tuesday, September 25, 2007

29

# Mutual Authentication

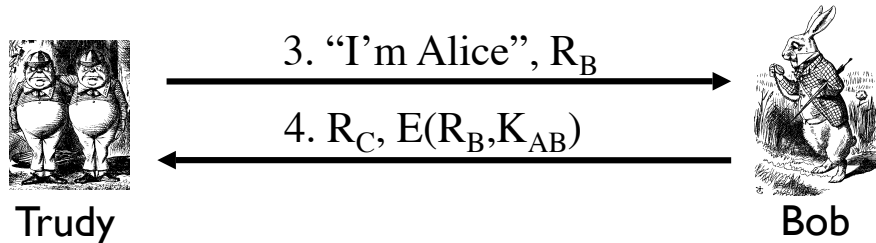
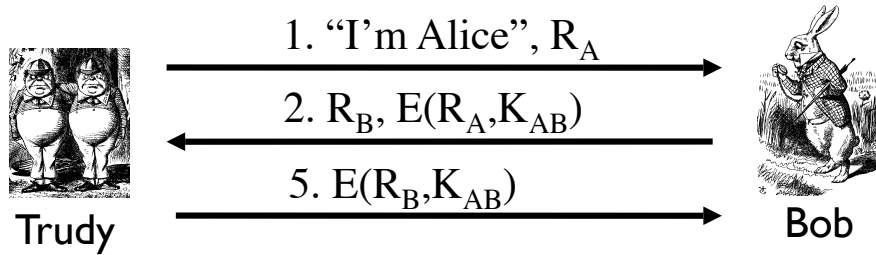


- This provides mutual authentication
- Is it secure? See the next slide...

Tuesday, September 25, 2007

30

# mutual authentication attack

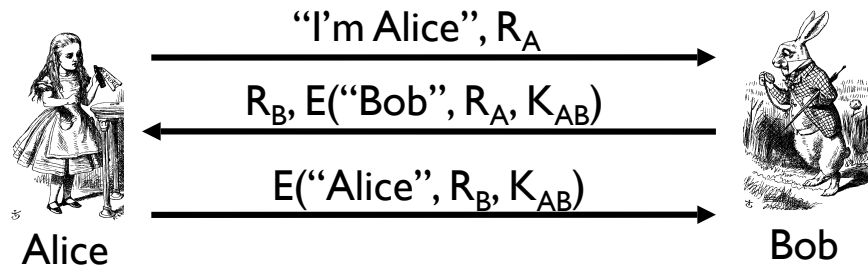


## Mutual Authentication

- Our one-way authentication protocol **not** secure for mutual authentication
- Protocols are subtle!
- The "obvious" thing may not be secure
- Also, if assumptions or environment changes, protocol may not work
  - This is a common source of security failure
  - For example, Internet protocols

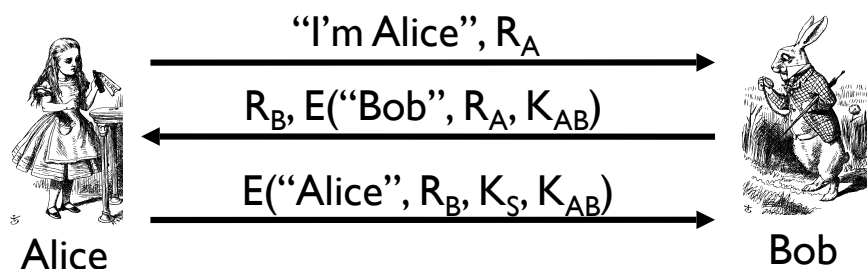


# mutual authentication with symmetric key



- Do these “insignificant” changes help?
- Yes!

# session key with mutual authentication using symmetric key



# Perfect Forward Secrecy

# Perfect Forward Secrecy

- The concern...
  - Alice encrypts message with shared key  $K_{AB}$  and sends ciphertext to Bob
  - Trudy records ciphertext and later attacks Alice's (or Bob's) computer to find  $K_{AB}$
  - Then Trudy decrypts recorded messages
- **Perfect forward secrecy (PFS):** Trudy cannot later decrypt recorded ciphertext
  - Even if Trudy gets key  $K_{AB}$  or other secret(s)
- Is PFS possible?

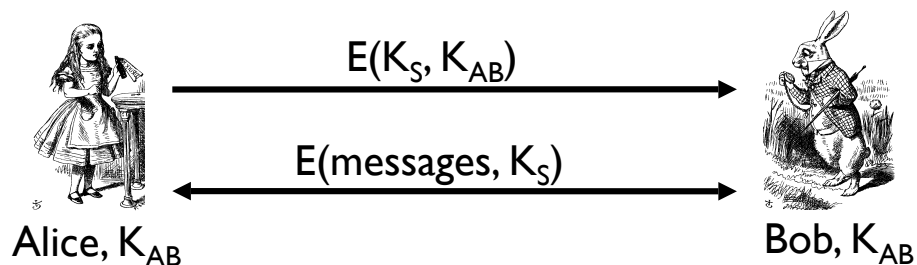
# Perfect Forward Secrecy

- For perfect forward secrecy, Alice and Bob cannot use  $K_{AB}$  to encrypt
- Instead they must use a **session key**  $K_S$  and forget it after it's used
- Problem: How can Alice and Bob agree on session key  $K_S$  and insure PFS?

Tuesday, September 25, 2007

37

## naïve session key protocol



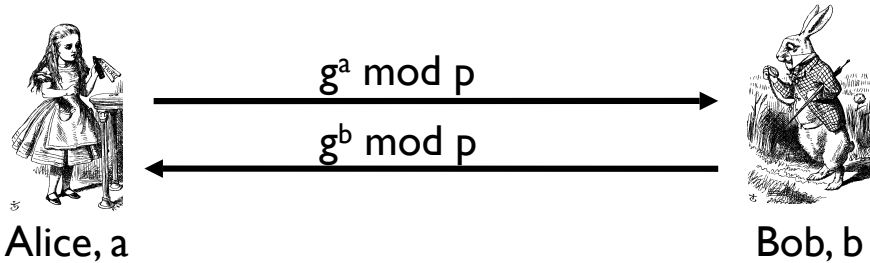
- Trudy could also record  $E(K_S, K_{AB})$
- If Trudy gets  $K_{AB}$ , she gets  $K_S$

Tuesday, September 25, 2007

38

# perfect forward secrecy

- Can use **Diffie-Hellman** for PFS
- Recall Diffie-Hellman: public  $g$  and  $p$

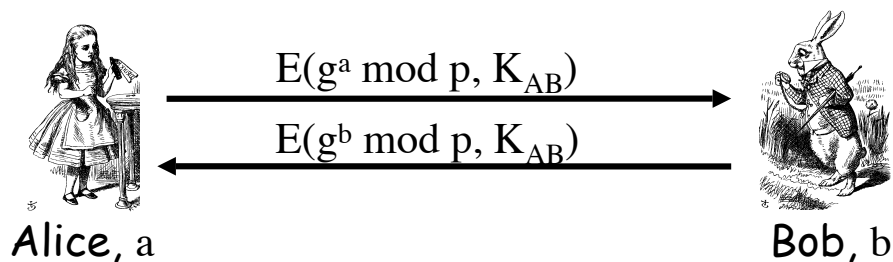


- But Diffie-Hellman is subject to MiM
- How to get PFS and prevent MiM?

Tuesday, September 25, 2007

39

# PFS session key via DH

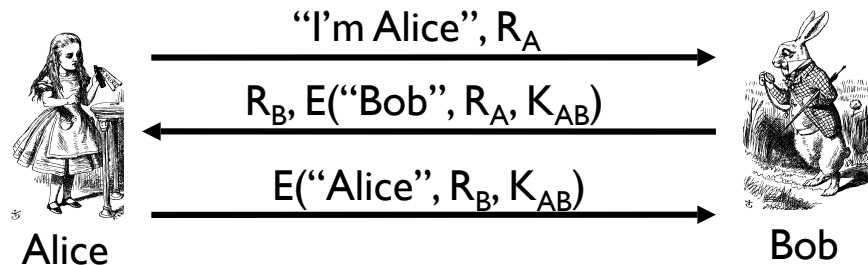


- Session key  $K_S = g^{ab} \bmod p$
  - Alice forgets  $a$ , Bob forgets  $b$
- Ephemeral Diffie-Hellman**
- Not even Alice and Bob can later recover  $K_S$
  - Other ways to do PFS?

Tuesday, September 25, 2007

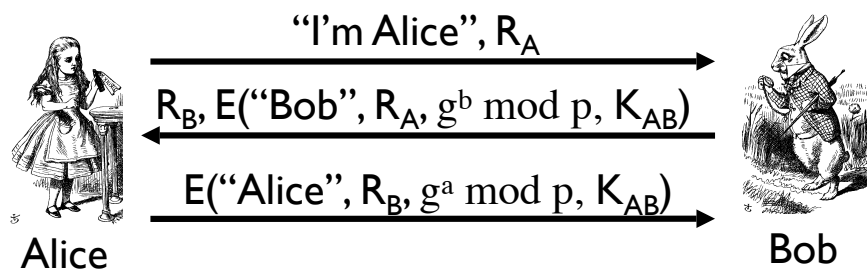
40

# mutual authentication with symmetric key



- Do these “insignificant” changes help?
- Yes!

# FPS session key with mutual authentication using symmetric key



# Outline

1. Diffie-Hellman key exchange (4.4)
2. mutual authentication in networks (9.1-9.3.3)
3. perfect forward secrecy (9.3.4, 9.3.5)