



THE UNIVERSITY OF BRITISH COLUMBIA

Introduction to Cryptography

Module Outline

- Historical background
 - Classic ciphers
 - One-time pad
- The Random Oracle model
 - Random functions: Hash functions
 - Random generators: stream ciphers
 - Random Permutations: block ciphers
 - Public key encryption and trapdoor one-way permutations
 - Digital signatures

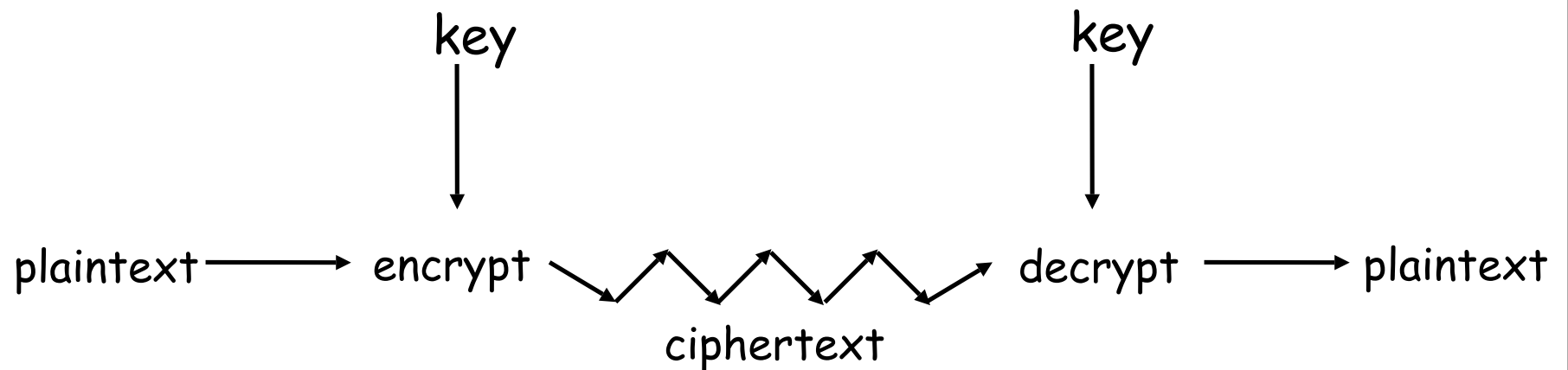
Crypto

- **Cryptology** — The art and science of making and breaking “secret codes”
- **Cryptography** — making “secret codes”
- **Cryptanalysis** — breaking “secret codes”
- **Crypto** — all of the above (and more)

How to Speak Crypto

- A *cipher* or *cryptosystem* is used to *encrypt* the *plaintext*
- The result of encryption is *ciphertext*
- We *decrypt* ciphertext to recover plaintext
- A *key* is used to configure a cryptosystem
- A *symmetric key* cryptosystem uses the same key to encrypt as to decrypt
- A *public key* cryptosystem uses a *public key* to encrypt and a *private key* to decrypt

Crypto as Black Box



A generic use of crypto

basic assumptions in crypto

- assumptions
 1. The system is completely known to the attacker
 2. Only the key is secret
- Also known as **Kerckhoffs Principle**
 - Crypto algorithms are not secret

Kerckhoff's Principle

“The security of a cryptosystem must not depend on keeping secret the crypto-algorithm. The security depends only on keeping secret the key”

Auguste Kerckhoff von Nieuwenhof

Dutch linguist

1883

basic assumptions in crypto

- assumptions
 1. The system is completely known to the attacker
 2. Only the key is secret
- Also known as **Kerckhoffs Principle**
 - Crypto algorithms are not secret
- Why do we make this assumption?
 - Experience has shown that secret algorithms are weak when exposed
 - Secret algorithms never remain secret
 - Better to find weaknesses beforehand

Historical Background

- To read:
- 5.1-5.2 Anderson's book
- Chapter 2 (except 2.3.6 & 2.3.8) Stamp's book

two types of ciphers

- substitution
- transposition

Letter Indices in English Alphabet

A	B	C	D	E	F	G	H	I	J	K	L	M
0	1	2	3	4	5	6	7	8	9	10	11	12

N	O	P	Q	R	S	T	U	V	W	X	Y	z
13	14	15	16	17	18	19	20	21	22	23	24	25

Caesar Cipher

- Plaintext is HELLO WORLD
- Change each letter to the third letter following it (X goes to A, Y to B, Z to C)
- Key is 3, usually written as letter 'D'
- **$C = P + K \text{ mod } 26$**
- Ciphertext: KHOOR ZRUOG

Plain HELLOWORLD

Key DDDDDDDDDD

Cipher KHOORZRUOG

a simple attack

- how to attack Caesar Cipher?
- exhaustive/brute-force (key) search
- Trudy 2^{40}
- 2^{56} -- 18 hours
- 2^{64} -- 6 months
- how to increase key space for substitution cipher?

Monoalphabetic Substitution Cipher

Invented by Arabs in 8th or 9th centuries

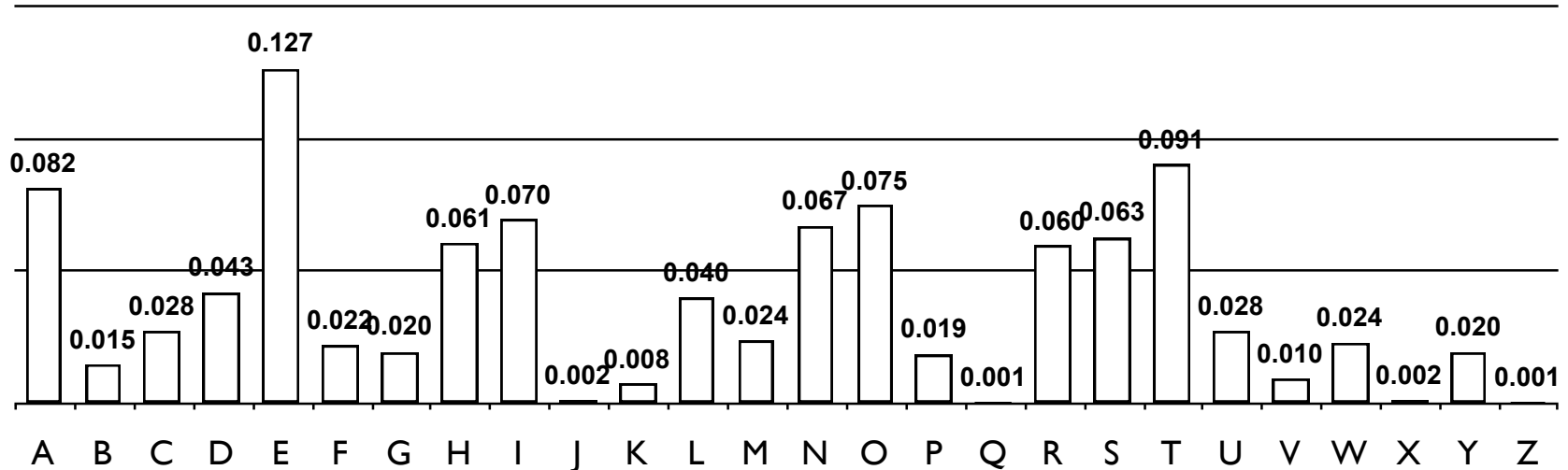
A	B	C	D	E	F	G	H	I	J	K	L	M	N	..	Z
F	T	W	S	G	M	P	A	Z	C	L	V	O	D	..	B

Plain HELLOWORLD

Key

Cipher AGVVYEYZVS

Frequency Analysis of English Letters



Polyalphabetic Vigenère Cipher

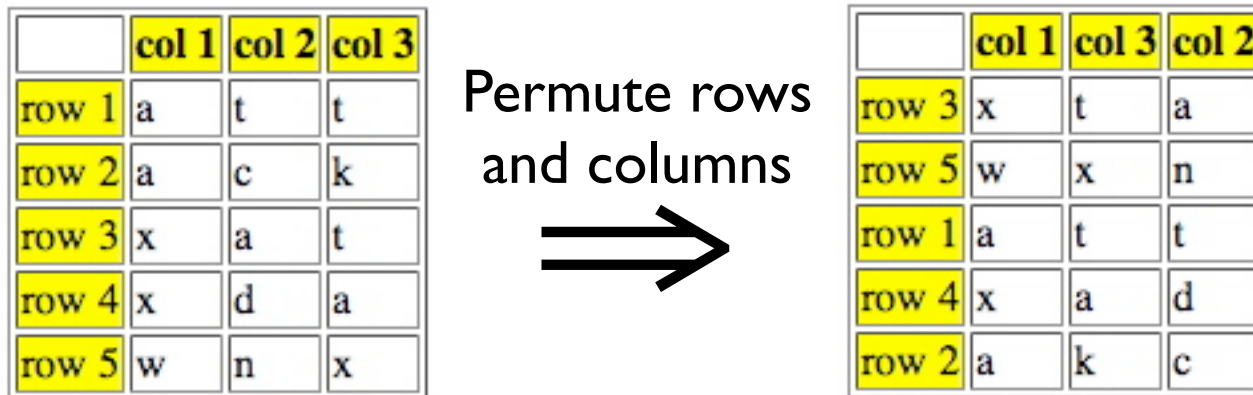
proposed by Blaise de Vigenere from the court of Henry III of France in the sixteenth century

Like Cæsar cipher, but use a phrase

- Example
 - Message: TO BE OR NOT TO BE THAT IS THE QUESTION
 - Key: RELATIONS
 - Encipher using Cæsar cipher for each letter:

Plain	TO BE OR NOT TO BE THAT IS THE QUESTION
Key	RE LA T I ONS RE LA T I ON SR ELA T I ONSREL
Cipher	KS ME HZ BBL KS ME MPOG AJ XSE J CSF LZSY

Double Transposition



- Plaintext: attackxatxdawn
- Ciphertext: xtawxnattxadakc
- Key: matrix size and permutations
(3,5,1,4,2) and (1,3,2)

Cryptanalysis: Terminology

- Cryptosystem is **secure** if best know attack is to try all keys
- Cryptosystem is **insecure** if any shortcut attack is known
- By this definition, an insecure system might be harder to break than a secure system!

One-Time Pad

A Vigenère cipher with a random key at least as long as the message

- Provably unbreakable
- Why?

Plain text	D O I T	D O N T
Key	A J I Y	A J D Y
Cipher text	D X Q R	D X Q R

- Warning: keys *must* be random, or you can attack the cipher by trying to regenerate the key

Little Bit of History

- 91 years ago,
January 19, 1917 ...

Codebook

- Literally, a book filled with “codewords”
- Zimmerman Telegram encrypted via codebook

Februar 13605

fest 13732

finanzielle 13850

folgender 13918

Frieden 17142

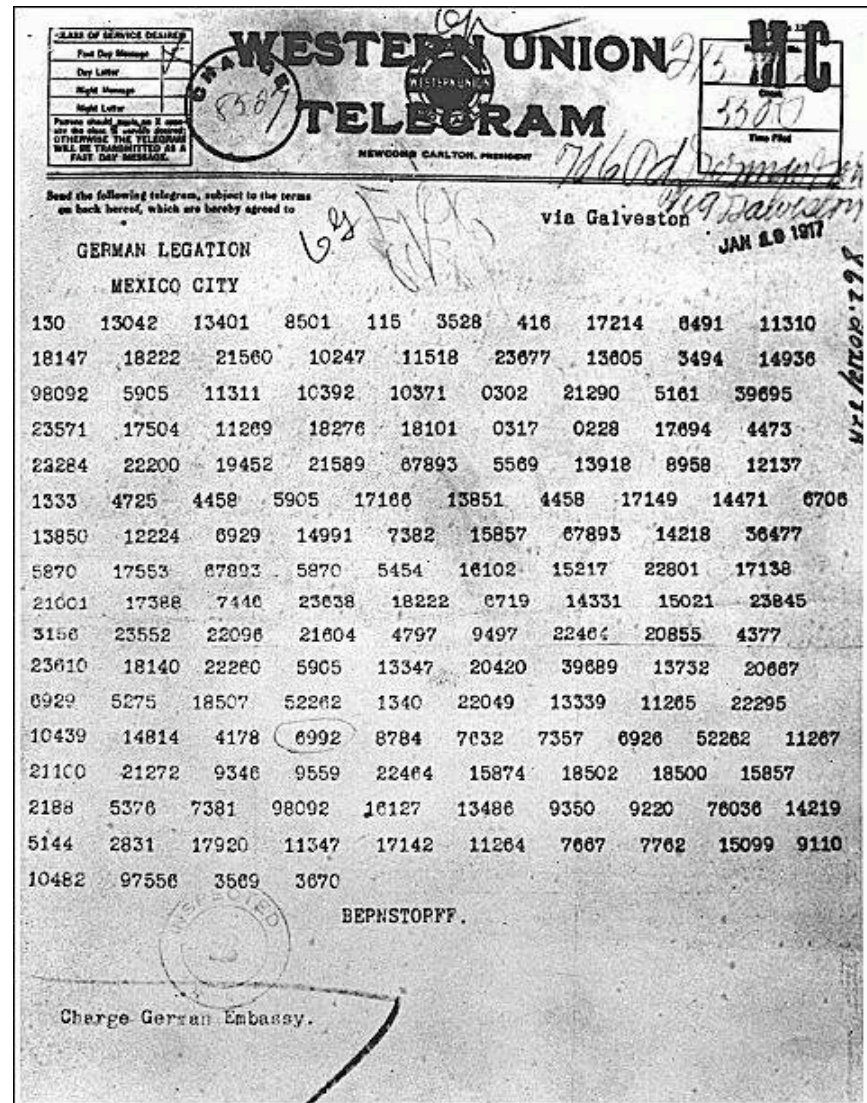
Friedenschluss 17149

: :

- Modern block ciphers are codebooks!

Zimmerman Telegram

- One of most famous codebook ciphers ever
- Led to US entry in WWI
- Ciphertext shown here...



Zimmerman Telegram Decrypted

- British had recovered partial codebook
- Able to fill in missing parts

TELEGRAM RECEIVED.

By *Walter A. Eckhoff* *Washington*
Date *Oct. 27, 1917*

FROM 2nd from London # 5747.

"We intend to begin on the first of February unrestricted submarine warfare. We shall endeavor in spite of this to keep the United States of America neutral. In the event of this not succeeding, we make Mexico a proposal of alliance on the following basis: make war together, make peace together, generous financial support and an understanding on our part that Mexico is to reconquer the lost territory in Texas, New Mexico, and Arizona. The settlement in detail is left to you. You will inform the President of the above most secretly as soon as the outbreak of war with the United States of America is certain and add the suggestion that he should, on his own initiative, ~~write~~ *invite* Japan to immediate adherence and at the same time mediate between Japan and ourselves. Please call the President's attention to the fact that the ruthless employment of our submarines now offers the prospect of compelling England in a few months to make peace." Signed, ZIMMERMAN.

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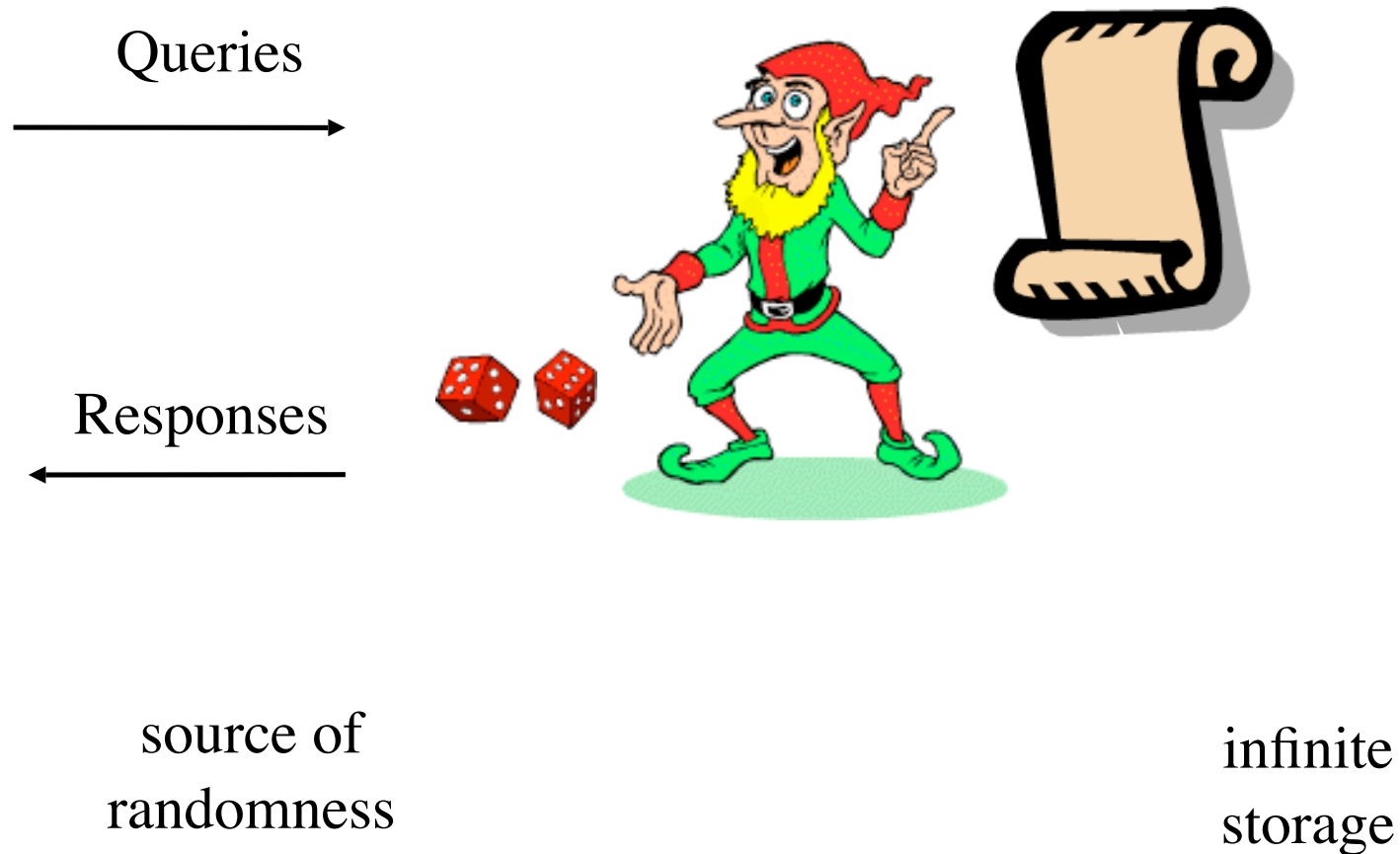


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Random Oracle Model

Read Anderson 5.3

What is Random Oracle Model?



Random Function as Random Oracle

- In: string of any length



- Out: random string of fixed length
- Applications:

- One-way functions
- Hash functions
 - Message digests
 - Time stamping

Properties

efficiency -- easy to compute $h(x)$ for any x .
one-way -- given any y , it's infeasible to find x , s.t., $h(x) = y$
weak collision resistance -- given x and $h(x)$, it's infeasible to $y \neq x$, s.t. $h(y) == h(x)$
strong collision resistance -- infeasible to find any $x \neq y$, s.t., $h(x) == h(y)$

Random Generator (Stream Cipher)

as Random Oracle

- In:
 - short string (key)
 - length of the output



- Out: long random stream of bits (keystream)

- Applications:

- Communications encryption
- Storage encryption

Properties

- Should not reuse
 - Use *seed*

Example: A5 stream cipher for GSM

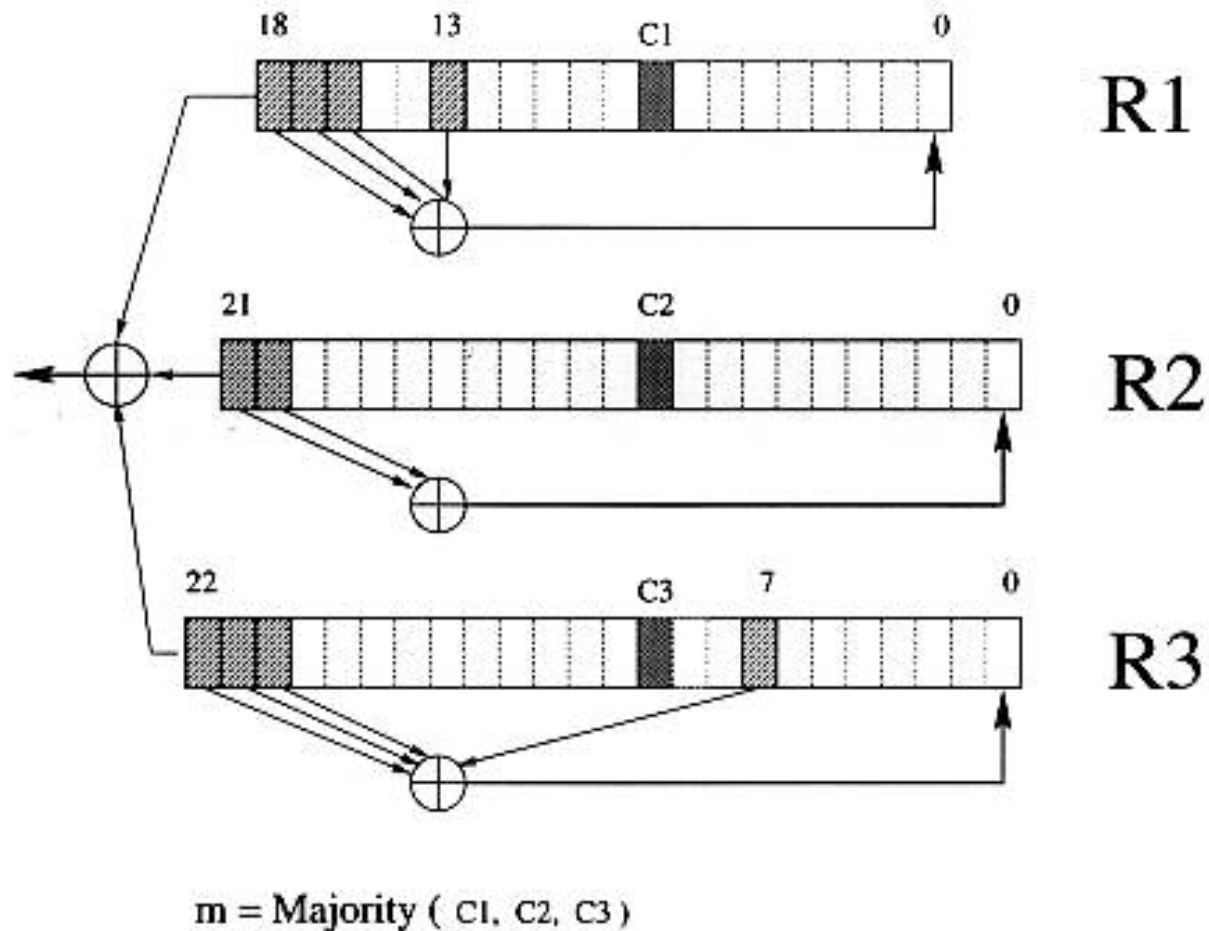


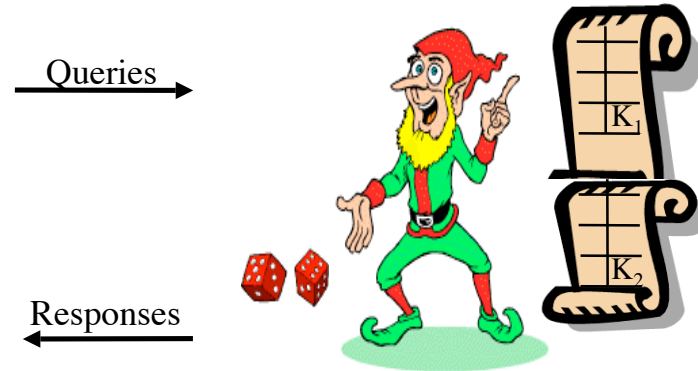
Figure 1: The A5/1 stream cipher.

From: Alex Biryukov, Adi Shamir, David Wagner "Real Time Cryptanalysis of A5/1 on a PC"

Random Permutation (Block Cipher)

as Random Oracle

- In
 - fixed size short string (plaintext) M ,
 - DES -- 64 bits
 - Key K



- Out
 - same fixed size short string (ciphertext) C

Notation

- $C = \{ M \}_K$
- $M = \{ C \}_K$

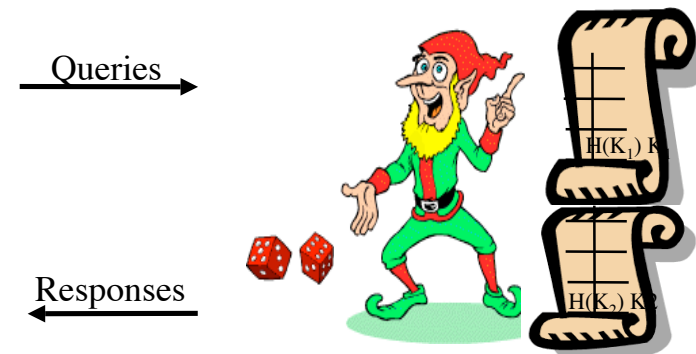
Properties

- Invertible

Public Key Encryption and Trap-door One-Way Permutation

as Random Oracle

- Public Key Encryption Scheme:
 - Key pair (KR, KR^{-1}) generation function from random string R
 - $KR \rightarrow KR^{-1}$ is infeasible
 - $C = \{M\}_{KR}$
 - $M = \{C\}_{KR^{-1}}$
 - In:
 - fixed size short string (plaintext) M ,
 - Key KR
 - Out: fixed size short string (ciphertext) C



Digital Signature as Random Oracle

- Public Key Signature Scheme:
 - Key pair $(\sigma R, VR)$ generation function
 - $VR \rightarrow \sigma R$ is infeasible
 - $S = \text{Sig}_{\sigma R}(M)$
 - $\{\text{True}, \text{False}\} = \text{Ver}_{VR}(S)$



	Signing	Verifying
Input	Any string $M + \sigma R$	$S + VR$
Output	$S = \text{hash}(M) \mid \text{cipher block}$	“True” or “False”

Summary

- Historical background
 - Caesar and Vigenère ciphers
 - One-time pad
 - One-way functions
 - Asymmetric cryptosystems
- The Random Oracle model
 - Random functions: Hash functions
 - Random generators: stream ciphers
 - Random Permutations: block ciphers
 - Public key encryption and trapdoor one-way permutations
 - Digital signatures

Queries →

← Responses

