



THE UNIVERSITY OF BRITISH COLUMBIA

# Introduction to Cryptography

# Module Outline

- Historical background
  - Classic ciphers
  - One-time pad
- The Random Oracle model
  - Random functions: Hash functions
  - Random generators: stream ciphers
  - Random Permutations: block ciphers
  - Public key encryption and trapdoor one-way permutations
  - Digital signatures

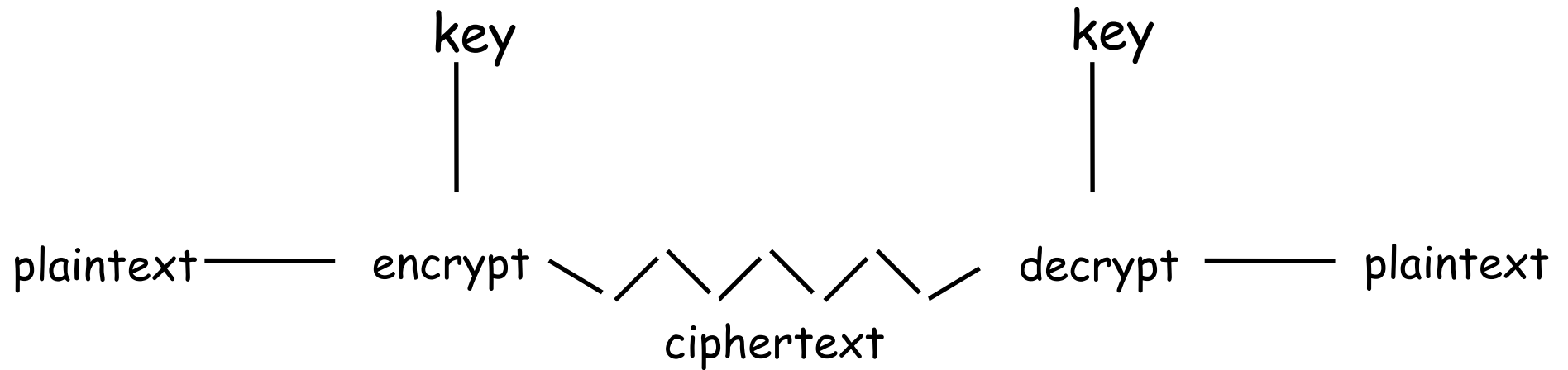
# Crypto

- **Cryptology** — The art and science of making and breaking “secret codes”
- **Cryptography** — making “secret codes”
- **Cryptanalysis** — breaking “secret codes”
- **Crypto** — all of the above (and more)

# How to Speak Crypto

- A *cipher* or *cryptosystem* is used to *encrypt* the *plaintext*
- The result of encryption is *ciphertext*
- We *decrypt* ciphertext to recover plaintext
- A *key* is used to configure a cryptosystem
- A *symmetric key* cryptosystem uses the same key to encrypt as to decrypt
- A *public key* cryptosystem uses a *public key* to encrypt and a *private key* to decrypt

# Crypto as Black Box



A generic use of crypto

# basic assumptions in crypto

- assumptions
  1. The system is completely known to the attacker
  2. Only the key is secret
- Also known as **Kerckhoffs Principle**
  - Crypto algorithms are not secret

# Kerckhoff's Principle

*“The security of a cryptosystem must not depend on keeping secret the crypto-algorithm. The security depends only on keeping secret the key”*

Auguste Kerckhoff von Nieuwenhof

Dutch linguist

1883

# basic assumptions in crypto

- assumptions
  1. The system is completely known to the attacker
  2. Only the key is secret
- Also known as **Kerckhoffs Principle**
  - Crypto algorithms are not secret
- Why do we make this assumption?
  - Experience has shown that secret algorithms are weak when exposed
  - Secret algorithms never remain secret
  - Better to find weaknesses beforehand



# Historical Background

- To read:
- 5.1-5.2 Anderson's book
- Chapter 2 (except 2.3.6 & 2.3.8) Stamp's book

# two types of ciphers

- substitution
- transposition

# Letter Indices in English Alphabet

A	B	C	D	E	F	G	H	I	J	K	L	M
0	1	2	3	4	5	6	7	8	9	10	11	12

N	O	P	Q	R	S	T	U	V	W	X	Y	z
13	14	15	16	17	18	19	20	21	22	23	24	25

# Caesar Cipher

- Plaintext is HELLO WORLD
- Change each letter to the third letter following it (X goes to A, Y to B, Z to C)
- Key is 3, usually written as letter 'D'
- $C = P + K \bmod 26$
- Ciphertext: KHOOR ZRUOG

Plain HELLOWORLD

Key DDDDDDDDDDD

Cipher KHOORZRUOG

# a simple attack

- how to attack Caesar Cipher?
- exhaustive/brute-force (key) search
- Trudy can try  $2^{40}$  candidates/second
- $2^{56}$  -- 18 hours
- $2^{64}$  -- 6 months
- how to increase key space for substitution cipher?

# Monoalphabetic Substitution Cipher

Invented by Arabs in 8th or 9th centuries

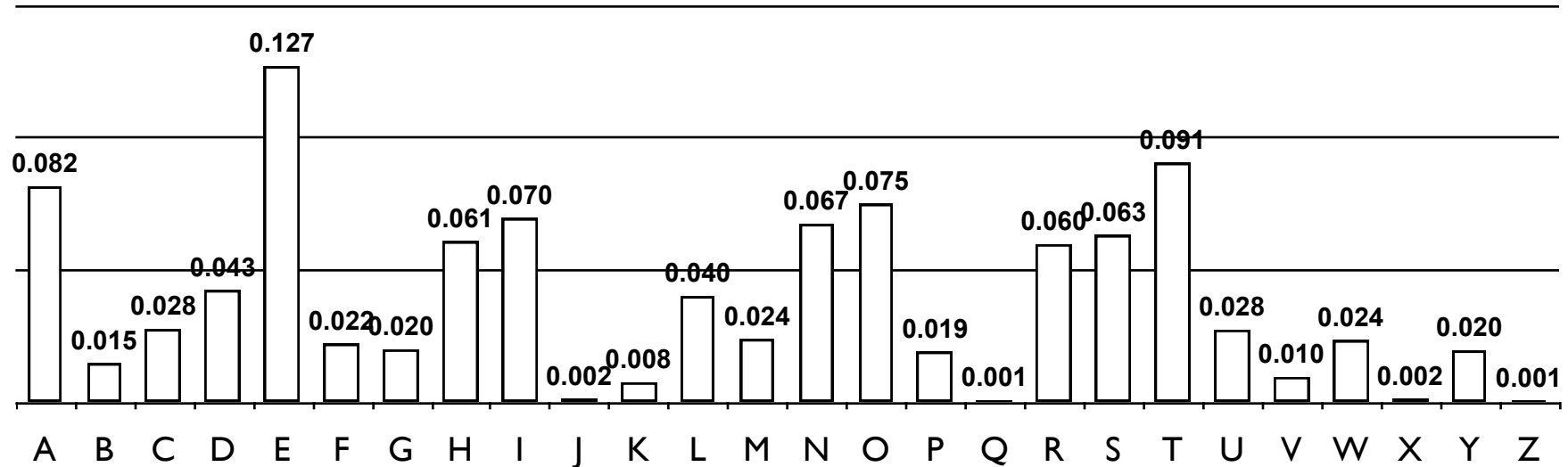
A	B	C	D	E	F	G	H	I	J	K	L	M	N	..	Z
F	T	W	S	G	M	P	A	Z	C	L	V	O	D	..	B

Plain      HELLOWORLD

Key

Cipher    AGVVYEYZVS

# Frequency Analysis of English Letters



# Polyalphabetic Vigenère Cipher

proposed by Blaise de Vigenere from the court of Henry III of France in the sixteenth century

Like Cæsar cipher, but use a phrase

- Example
  - Message: TO BE OR NOT TO BE THAT IS THE QUESTION
  - Key: RELATIONS
  - Encipher using Cæsar cipher for each letter:

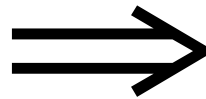
Plain	TO BE OR NOT TO BE THAT IS THE QUESTION
Key	RE LA T I ONS RE LA T I ONS SR ELA T I ONSREL
Cipher	KS ME HZ BBL KS ME MPOG AJ XSE J CSF LZSY



# Double Transposition

	col 1	col 2	col 3
row 1	a	t	t
row 2	a	c	k
row 3	x	a	t
row 4	x	d	a
row 5	w	n	x

Permute rows  
and columns



	col 1	col 3	col 2
row 3	x	t	a
row 5	w	x	n
row 1	a	t	t
row 4	x	a	d
row 2	a	k	c

- Plaintext: attackxatxdawn
- Ciphertext: xtawxnatxadakc
- Key: matrix size and permutations  
(3,5,1,4,2) and (1,3,2)

# Cryptanalysis: Terminology

- Cryptosystem is **secure** if best known attack is to try all keys
- Cryptosystem is **insecure** if any shortcut attack is known
- By this definition, an insecure system might be harder to break than a secure system!

# One-Time Pad

A Vigenère cipher with a random key at least as long as the message

- Provably unbreakable
- Why?

Plain text	D O I T	D O N T
Key	A J I Y	A J D Y
Cipher text	D X Q R	D X Q R

- Warning: keys *must* be random, or you can attack the cipher by trying to regenerate the key

# Little Bit of History

- 91 years ago,  
January 19, 1917 ...

# Codebook

- Literally, a book filled with “codewords”
- Zimmerman Telegram encrypted via codebook

Februar            13605

fest                13732

finanzielle       13850

folgender         13918

Frieden            17142

Friedenschluss   17149

                  :

- Modern block ciphers are codebooks!

# Zimmerman Telegram



Arthur Zimmermann (1854-1940)  
German Foreign Secretary

- One of most famous codebook ciphers ever
- Led to US entry in WWI
- Ciphertext shown here...

WESTERN UNION TELEGRAM

NEW YORK CARLTON, PENNSYLVANIA

Send the following telegram, subject to the terms on back hereof, which are hereby agreed to

via Galveston

JAN 18 1917

GERMAN LEGATION  
MEXICO CITY

130	13042	13401	8501	115	3528	416	17214	8491	11310
18147	18222	21560	10247	11518	23877	13805	3494	14938	
98092	5905	11311	10392	10371	0302	21290	5161	39695	
23571	17504	11269	18276	18101	0317	0228	17694	4473	
23284	22200	19452	21589	87893	5589	13918	8958	12137	
1333	4725	4458	5905	17188	13851	4458	17149	14471	8708
13850	12224	6929	14991	7382	15857	87893	14218	36477	
5870	17553	87893	5870	5454	16102	15217	22801	17138	
21001	17388	7440	23838	18222	8719	14331	15021	23845	
3158	23552	22096	21604	4797	9497	22404	20855	4377	
23610	18140	22280	5905	13347	20420	39889	13732	20887	
6929	5275	18507	52282	1340	22049	13339	11265	22295	
10439	14814	4178	8992	8784	7832	7357	6926	52282	11287
21100	21272	9348	9559	22404	15874	18502	18500	15857	
2188	5376	7381	98092	16127	13486	9350	9220	76036	14219
5144	2831	17920	11347	17142	11284	7667	7762	15099	9110
10482	97558	3589	3870						

Charge German Embassy.

BEPNSTOPFF.

# Zimmerman Telegram Decrypted

- British had recovered partial codebook
- Able to fill in missing parts

MAILED  
October 1-8-08  
W. L. Garrison, State Dept.

TELEGRAM RECEIVED.

By *Wm. A. Eckhoff*  
Date *Oct 27, 1917*

FROM 2nd from London # 5747.

"We intend to begin on the first of February unrestricted submarine warfare. We shall endeavor in spite of this to keep the United States of America neutral. In the event of this not succeeding, we make Mexico a proposal of alliance on the following basis: make war together, make peace together, generous financial support and an understanding on our part that Mexico is to reconquer the lost territory in Texas, New Mexico, and Arizona. The settlement in detail is left to you. You will inform the President of the above most secretly as soon as the outbreak of war with the United States of America is certain and add the suggestion that he should, on his own initiative, ~~write~~ <sup>invite</sup> Japan to immediate adherence and at the same time mediate between Japan and ourselves. Please call the President's attention to the fact that the ruthless employment of our submarines now offers the prospect of compelling England in a few months to make peace." Signed, ZIMMERMAN.

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