# Introduction to Cryptography 

EECE 412

## Module Outline

- Historical background
- Classic ciphers
- One-time pad
- The Random Oracle model
- Random functions: Hash functions
- Random generators: stream ciphers
- Random Permutations: block ciphers


## learning objectives

- explain classic ciphers covered in the lectures
- encrypt and decrypt using these classic cyphers
- break classic ciphers (home assignment \#2)
- explain one-time-pad and encrypt/decrypt wit it
- explain the Random Oracle Models for hash function, stream cipher, and block cipher


## Crypto

- Cryptology - The art and science of making and breaking "secret codes"
- Cryptography — making "secret codes"
- Cryptanalysis — breaking "secret codes"
- Crypto - all of the above (and more)


## How to Speak Crypto

- A cipher or cryptosystem is used to encrypt the plaintext
- The result of encryption is ciphertext
- We decrypt ciphertext to recover plaintext
- A key is used to configure a cryptosystem
- A symmetric key cryptosystem uses the same key to encrypt as to decrypt
- A public key cryptosystem uses a public key to encrypt and a private key to decrypt


## Crypto as Black Box


plaintext $\longrightarrow$ encrypt

decrypt $\longrightarrow$ plaintext

A generic use of crypto

## basic assumptions in crypto

- assumptions
I. The system is completely known to the attacker

2. Only the key is secret

- Also known as Kerckhoffs Principle
- Crypto algorithms are not secret


## Kerckhoff's Principle

"The security of a cryptosystem must not depend on keeping secret the crypto-algorithm. The security depends only on keeping secret the key"

Auguste Kerckhoff von Nieuwenhof
Dutch linguist
1883

## basic assumptions in crypto

- assumptions
I. The system is completely known to the attacker

2. Only the key is secret

- Also known as Kerckhoffs Principle
- Crypto algorithms are not secret
- Why do we make this assumption?
- Experience has shown that secret algorithms are weak when exposed
- Secret algorithms never remain secret
- Better to find weaknesses beforehand


## Historical Background

To read:
All of chapter 2
except 2.3.6 \& 2.3.8, which are optional reading

## two types of ciphers

- substitution
- transposition


## Letter Indices in English Alphabet

| A | B | C | D | E | F | G | H | I | J | K | L | M |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | I | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | IO | II | I2 |


| N | O | P | Q | R | S | T | U | V | W | X | Y | z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I 3 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

## Caesar Cipher

- Plaintext is HELLO WORLD
- Change each letter to the third letter following it ( $X$ goes to $A, Y$ to $B, Z$ to $C$ )
- Key is 3 , usually written as letter ' $D$ '
- C = P + K mod 26
- Ciphertext: KHOOR ZRUOG

Plain HELLOWORLD
Key DDDDDDDDDD
Cipher KHOORZRUOG

## a simple attack

- how to attack Caesar Cipher?
- exhaustive/brute-force (key) search
- with 26 keys, how many attempts on average?
- Trudy can try $2^{40}$ candidates/second
- $2^{56}$-- 18 hours
- $2^{64}$-- 6 months
- how to increase key space for substitution cipher?


## Monoalphabetic Substitution

 CipherInvented by Arabs in 8th or 9th centuries

| A | B | C | D | E | F | G | H | I | J | K | L | M | N | . | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| F | T | W | S | G | M | P | A | Z | C | L | V | O | D | .. | B |

Plain HELLOWORLD
Key
Cipher AGVVYEYZVS

## Frequency Analysis of English Letters



A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

## Polyalphabetic Vigenère Cipher

proposed by Blaise deVigenere from the court of Henry III of France in the sixteenth century
Like Cæsar cipher, but use a phrase

- Example
- Message: to be or not to be that is the question
- Key: relations
- Encipher using Cæsar cipher for each letter:

Plain TO BE OR NOT TO BE TH AT IS THE QUESTION
Key
Cipher KS ME HZ BBL KS ME MPOG AJ XSE J CSF LZSY

## Playfair Cipher

## background

- encrypts pairs of letters (digraphs), instead of single letters
- $\sim 600$ possible digraphs rather than the 26 possible monographs
- was used for tactical purposes by
- British forces in the Second Boer War (in South Africa) and in World War I
- the Australians and Germans during World War II


## anecdotal history

- invented in 1854 by Charles Wheatstone
- rejected by the British Foreign Office when it was developed because of its perceived complexity
- Wheatstone offered to demonstrate that
 three out of four boys in a nearby school could learn to use it in 15 minutes
- the Under Secretary of the Foreign Office responded: "That is very possible, but you could never teach it to attachés."
- named after Lord Playfair who promoted the use of the cipher


## setting up the cipher

- $5 \times 5$ table
- key example:
"playfair example"
- drop any duplicate letters
- fill the remaining of the letters from English the alphabet / one letter ( f or Q )

$$
\begin{array}{lllll}
\mathbf{P} & \mathbf{L} & \mathbf{A} & \mathbf{Y} & \mathbf{F} \\
\mathbf{I} & \mathbf{R} & \mathbf{E} & \mathbf{X} & \mathbf{M}^{2 \mathrm{LE}} \\
\mathbf{B} & \mathbf{C} & \mathbf{D} & \mathbf{G} & \mathbf{H}=J \\
\mathbf{K} & \mathbf{N} & \mathbf{O} & \mathbf{Q} \\
\mathbf{T} & \mathbf{U} & \mathbf{V} & \mathbf{W} & \mathbf{Z}
\end{array}
$$

## encryption overview

I. break the plain text into digraphs
I. append " $X$ " if odd number of characters.
2. split double letters with "X", e.g.,"EE" -> "EXE"
3. "Hide the gold in the tree stump" becomes "HI DETH EG OL DI NT HETR EX ES TU MP"
2. map each digraph out using the table

## mapping rules

If a pair forms a rectangle, replace it with letters from the opposite corners on the same row.

$$
\begin{array}{lllll}
\mathrm{P} & \mathrm{~L} & \mathrm{~A} & \mathrm{Y} & \mathrm{~F} \\
\hline \mathrm{I} & \mathrm{R} & \mathrm{~F} & \mathrm{X} & \mathrm{M} \\
\mathrm{~B} & \mathrm{C} & \mathrm{D} & \mathrm{G} & \mathrm{H}
\end{array}
$$

## HI

Shape: Rectangle
Rule: Pick Same Rows,

$$
K N O Q S
$$ Opposite Corners

T U V W Z

BM

## mapping rules

If the letters appear on the same column of your table, replace them with the letters immediately below respectively.

$$
\begin{array}{llllll}
\mathbf{P} & \mathrm{L} & \mathbf{A} & \mathbf{Y} & \mathrm{~F} & \mathrm{DE}
\end{array}
$$

$$
\begin{array}{ll|l|ll}
\mathbf{I} & \mathrm{R} & \underset{\mathrm{E}}{\mathrm{X}} & \mathbf{M} \\
\mathrm{~B} & \mathbf{C} & \underset{\mathrm{D}}{ } & \mathbf{G} & \mathrm{H}
\end{array}
$$

Shape: Column
Rule: Pick Items Below Each Letter, Wrap to Top if Needed

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

## "HI DE THEG OL DI NT HETR EX ESTU MP" "BM OD ? ? ...

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

# "HI DE TH EG OL DI NT HETR EX ESTU MP" "BM OD ZB ?? ... 

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

# "HI DE TH EG OL DI NT HETR EX ESTU MP" "BM OD ZB XD ? ? ... 

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

# "HI DE TH EG OL DI NT HETR EX ESTU MP" "BM OD ZB XD NA ?? ... 

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

# "HI DE TH EG OL DI NT HETR EX ESTU MP" "BM OD ZB XD NA BE ? ?... 

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

# "HI DE TH EG OL DI NT HETR EX ESTU MP" "BM OD ZB XD NA BE KU ? ? ... 

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

## "HI DE THEG OL DI NT HE TR EX ESTU MP" "BM OD ZB XD NA BEKU DM ? ? ...

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

# "HI DE THEG OL DINT HE TR EX ESTU MP" "BM OD ZB XD NA BE KU DMUI??... 

If the letters appear on the same row of your table, replace them with the letters immediately to right, respectively.Wrap to left, if needed.

## P L A Y F

I R E $>\mathbf{X}>\mathrm{M}$

## EX

Shape: Row
Rule: Pick Items to Right of Each Letter, Wrap to Left if Needed
K N O Q S
T U V W Z

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

"HI DE THEG OL DINT HE TREX ES TU MP"
"BM OD ZB XD NA BE KU DM UI XM ? ?..

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

"HI DE TH EG OL DI NT HE TR EX ES TU MP" "BM OD ZB XD NA BE KU DM UI XM MO ? ? ...

| P | L | A | Y | F |
| :---: | :---: | :---: | :---: | :---: |
| I | R | E | X | M |
| B | C | D | G | H |
| K | N | O | Q | S |
| T | U | V | W | Z |

"HI DE THEG OL DI NT HE TR EX ES TU MP" "BM OD ZB XD NA BE KU DM UI XM MO UV ? ? ...
"HIDE THE GOLD IN THE TREE STUMP"
"HI DE THEG OL DI NT HE TR EX ES TU MP" "BM OD ZB XD NA BE KU DM UI XM MO UV IF"
-How to decrypt it with the key?
-What betrays Palyfair?
-How can one break it?

## Double Transposition

|  | col 1 | col 2 | $\operatorname{col}$ 3 |
| :--- | :--- | :--- | :--- |
| row 1 | a | t | t |
| row 2 | a | c | k |
| row 3 | x | a | t |
| row 4 | x | d | a |
| row 5 | w | n | x |


| Permute rows and columns |  | col 1 | col 3 | col 2 |
| :---: | :---: | :---: | :---: | :---: |
|  | row 3 | x | t | a |
|  | row 5 | w | X | n |
|  | row 1 | a | t | t |
|  | row 4 | X | a | d |
|  | row 2 | a | k | c |

- Plaintext: attackxatxdawn
- Ciphertext: xtawxnattxadakc
- Key: matrix size and permutations (3,5, $1,4,2$ ) and ( $1,3,2$ )


## Cryptanalysis:Terminology

- Cryptosystem is secure if best known attack is to try all keys
- Cryptosystem is insecure if any shortcut attack is known
- By this definition, an insecure system might be harder to break than a secure system! Why?


## one-time pad (OTP)

## One-Time Pad

A Vigenère cipher with a random key at least as long as the message

- Provably unbreakable
- Why?

| Plain text | D O I T | D ONT |
| :---: | :---: | :---: |
| Key | A J I Y | A J DY |
| Cipher text | D Q R | D $\times$ Q R |

- Warning: keys must be random, or you can attack the cipher by trying to regenerate the key


## Little Bit of History

- about 95 years ago, January 19, I9|7 ...


## Codebook

- Literally, a book filled with "codewords"
- Zimmerman Telegram encrypted via codebook

| Februar | I3605 |
| :--- | :--- |
| fest | 13732 |

finanzielle I3850
folgender |3918
Frieden I7142
Friedenschluss I7149

- Modern block ciphers are codebooks!


## Zimmerman Telegram



Arthur Zimmermann (I854-I940)
German Foreign Secretary

- One of most famous codebook ciphers ever
- Led to US entry in WWI
- Ciphertext shown here...



## Zimmerman Telegram Decrypted

## - British had recovered partial codebook <br> - Able to fill in missing parts

## A. CSLED <br> TELEEGRAM RECEIVED.

- .otor $1-8-88$

FROM 2nd from London 5747.
м Mucher Enthef chiliunit Batect 20,14 ?
"We intend to begin on the first of February unrestricted submarine wariare. We shall endeavo in spite of this to keep the United States of merica neutral. In the event of this not succeeding, we make Mexico a proposal of alliance on the following basia: make war together, make peace together, generous ifnancial support and an understanding on our part that Mexico is to reconquer the loet territory in Texas, New Mexico, and arizona. The settlement in detail is left to you. You will inform the President of the above most secretly as soon as the outbreak of war with the United States of America is certain and add the suggestion that he should, on his own initiative, invile Japan to immediate adherence and at the rame time mediate between Japan and ourselves. Please csil the President's attention to the fact that the ruthless employment of our submarines now offers the prospect of compelling England in a few months to make peace." siened, ZIi : \&RAM.

# Random Oracle Model 

Read Anderson 5.3 from (First Edition) http://www.cl.cam.ac.uk/~rjal 4/book.html

## What is Random Oracle Model?



## Random Function as Random Oracle

- In: string of any length

- Out: random string of fixed length
- Applications:
- One-way functions
- Hash functions
- Message digests
- Time stamping


## Properties

efficiency -- easy to compute $h(x)$ for any $x$. one-way -- given any $y$, it's infeasible to find x, s.t., $\mathrm{h}(\mathrm{x})=\mathrm{y}$
weak collision resistance -- given $x$ and $h(x)$, it's infeasible to $y!=x$, s.t. $h(y)==h(x)$ strong collision resistance -- infeasible to find any $x!=y$, s.t., $h(x)==h(y)$

## Random Generator (Stream Cipher)

as Random Oracle

- In:
- short string (key)
- length of the output

- Out:long random stream of bits (keystream)
- Applications:
- Communications encryption
- Storage encryption

Properties

- Should not reuse
- Use seed


## Example:A5 stream cipher for GSM



Figure 1: The A5/1 stream cipher.
From:Alex Biryukov, Adi Shamir, David Wagnê" "Real Time Cryptanalysis of A5/I on a PC"

## Random Permutation (Block Cipher)

as Random Oracle


- In
- fixed size short string (plaintext) M,
- DES -- 64 bits

Responses


- Key K

Notation

- $C=\{M\}_{K}$
- $M=\{C\}_{K}$

Properties

- Invertible


## Summary

- Historical background
- Caesar, Vigenère, Palyfair, and Double Transpositionciphers
- One-time pad
- One-way functions

- Asymmetric cryptosystems
- The Random Oracle model
- Random functions: Hash functions
- Random generators: stream ciphers
- Random Permutations: block ciphers

