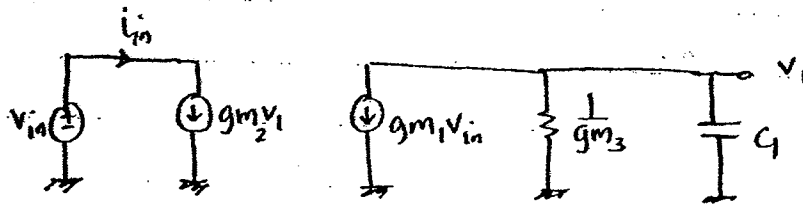


5.19 small signal model.



$$Z_{in} = \frac{v_{in}}{i_{in}} = \frac{v_{in}}{gm_2 v_1} \quad v_1 = -gm_1 \left(\frac{1}{C_1 + gm_3} \right) v_{in}$$

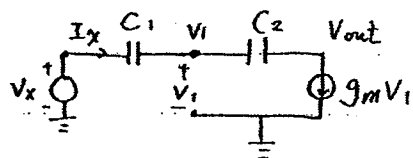
$$= - \frac{C_1 + gm_3}{gm_2 gm_1}$$

if all transistors are equal
 $gm_1 = gm_2 = gm_3$

$$Z_{in} = - \frac{C_1}{gm^2} - \frac{1}{gm}$$

negative $C = -\frac{C_1}{gm^2}$ and negative $R = \frac{1}{gm}$.

6.6(a)



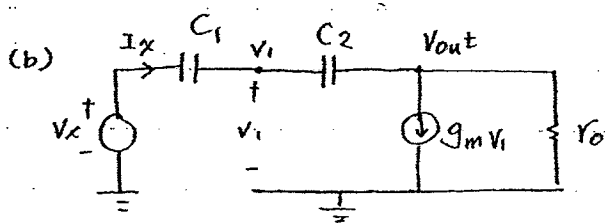
g_m : transconductance of M_1 .

$$I_x = sC_1(V_x - V_1) = sC_2(V_1 - V_{out}) = g_m V_1$$

$$\therefore sC_1 V_x = (g_m + sC_1) V_1 \Rightarrow V_1 = \left[\frac{sC_1}{g_m + sC_1} \right] V_x$$

$$\Rightarrow I_x = g_m V_1 = \left[\frac{g_m sC_1}{g_m + sC_1} \right] V_x$$

$$\Rightarrow Z_{in} = \frac{V_x}{I_x} = \frac{g_m + sC_1}{g_m sC_1} *$$



$$g_m = g_{m1} + g_{m2}$$

$$r_o = r_{o1} \parallel r_{o2}$$

g_{m1}, g_{m2} : transconductance for M_1, M_2

r_{o1}, r_{o2} : output resistance for M_1, M_2

$$\therefore I_x = sC_1(V_x - V_1) = \frac{sC_2(V_1 - V_{out})}{\text{①}} = \frac{g_m V_1 + \frac{V_{out}}{r_o}}{\text{②}}$$

from ① :

$$\frac{V_{out}}{V_1} = \frac{sC_2 - g_m}{sC_2 + \frac{1}{r_o}}$$

from ② :

$$(sC_1 + sC_2) V_1 = sC_1 V_x + sC_2 V_{out}$$

$$= sC_1 V_x + \frac{s^2 C_2^2 - g_m sC_2}{sC_2 + \frac{1}{r_o}} V_1$$

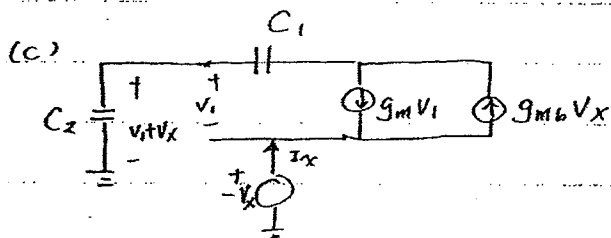
$$\Rightarrow \left[sC_1 + sC_2 - \frac{s^2 C_2^2 - g_m sC_2}{sC_2 + \frac{1}{r_o}} \right] V_1 = sC_1 V_x$$

$$\Rightarrow \left[\frac{sC_1C_2 + \frac{SC_1}{r_o} + \frac{SC_2}{r_o} + g_m sC_2}{sC_2 + \frac{1}{r_o}} \right] V_1 = sC_1 V_x$$

$$\therefore V_1 = \left[\frac{sC_1C_2 + \frac{C_1}{r_o}}{sC_1C_2 + \frac{C_1}{r_o} + \frac{C_2}{r_o} + g_m C_2} \right] V_x$$

$$I_x = sC_1(V_x - V_1) = sC_1 \cdot \left[\frac{\frac{C_2}{r_o} + g_m C_2}{sC_1C_2 + \frac{C_1}{r_o} + \frac{C_2}{r_o} + g_m C_2} \right] V_x$$

$$Z_{in} = \frac{V_x}{I_x} = \frac{sC_1C_2 + \frac{C_1}{r_o} + \frac{C_2}{r_o} + g_m C_2}{sC_1C_2 \left(\frac{1}{r_o} + g_m \right)}$$



$$sC_2(V_1 + V_x) + g_m V_1 = g_{mb} V_x$$

$$\Rightarrow (sC_2 + g_m)V_1 = (g_{mb} - sC_2)V_x$$

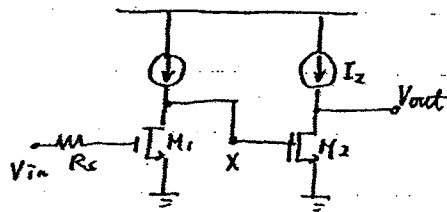
$$\frac{V_x}{V_1} = \frac{sC_2 + g_m}{g_{mb} - sC_2}$$

$$I_x = -g_m V_1 + g_{mb} V_x$$

$$= \left[-g_m \cdot \frac{g_{mb} - sC_2}{sC_2 + g_m} + g_{mb} \right] V_x = \left[\frac{(g_m + g_{mb})sC_2}{sC_2 + g_m} \right] V_x$$

$$Z_{in} = \frac{V_x}{I_x} = \frac{sC_2 + g_m}{sC_2(g_m + g_{mb})}$$

6.7(a)



There are three poles associated with this circuit.

The first pole @ V_{out}

$$\omega_{pout} = \frac{1}{r_{o2} \cdot (C_{gd2} + C_{db2})}$$

The pole @ the input

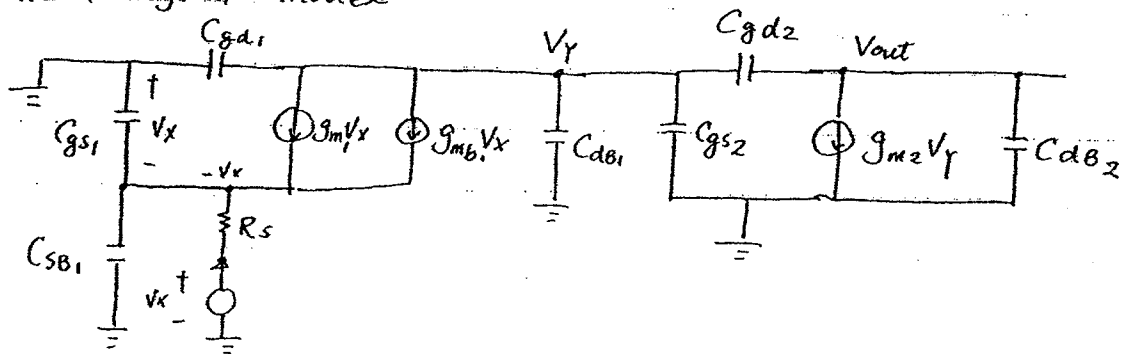
$$\omega_{p,in} = \frac{1}{R_s \cdot [(1 + g_{m1} r_{o1}) C_{gd1} + C_{gs1}]}$$

The pole @ node X

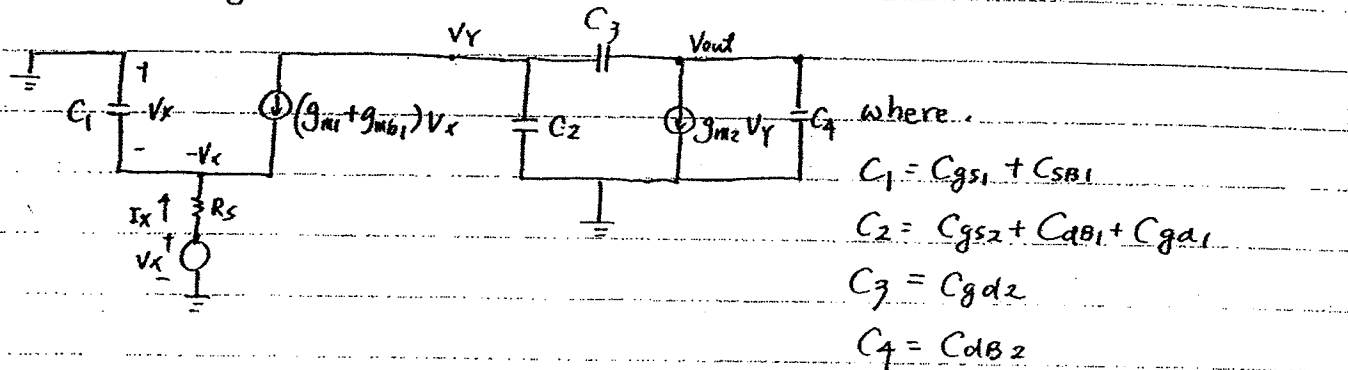
$$\omega_{p,X} = \frac{1}{r_{o1} \cdot [(C_{gd1} + C_{db1} + C_{gs2}) + (1 + g_{m2} r_{o1}) \cdot C_{gd2}]}$$

Please note that the above approximation is based on Miller effect. In order to get more accuracy approximation, transfer function has to be derived.

(b) Small signal model



Redraw small signal model



$$\text{KCL @ } V_{out} : S C_3 (V_Y - V_{out}) = g_{m2} V_Y + S C_4 V_{out}$$

$$\Rightarrow \frac{V_{out}}{V_Y} = \frac{-g_{m2} + S C_3}{S (C_3 + C_4)}$$

$$\text{KCL @ } V_Y : (g_{m1} + g_{mb1}) V_X + S C_2 V_Y + S C_3 (V_Y - V_{out}) = 0$$

$$(g_{m1} + g_{mb1}) V_X = -V_Y \left(-S C_2 + \frac{S^2 C_3 C_4 + S C_3 g_{m2}}{S (C_3 + C_4)} \right)$$

$$\frac{V_Y}{V_X} = \frac{g_{m1} + g_{mb1}}{[S(C_2 C_3 + C_2 C_4 + C_3 C_4) + C_3 g_{m2}] / (C_3 + C_4)}$$

$$\text{KCL @ } V_X : \frac{V_{in} + V_X}{R_S} + S C_1 V_X + (g_{m1} + g_{mb1}) V_X = 0$$

$$\frac{V_X}{V_{in}} = \frac{1}{S C_1 R_S + (1 + (g_{m1} + g_{mb1}) \cdot R_S)}$$

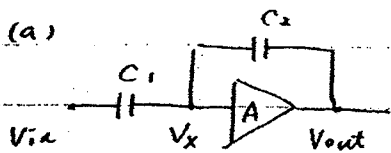
Thus, there are three poles

$$\omega_{p0} = 0$$

$$\omega_{p1} = \frac{-C_3 g_{m2}}{C_2 C_3 + C_2 C_4 + C_3 C_4} \quad *$$

$$\omega_{p2} = \frac{-(1 + (g_{m1} + g_{mb1}) \cdot R_S)}{C_1 R_S} \quad *$$

6.9 (a)



$$A = -\infty$$

(i) At low frequency, V_x is like virtual ground

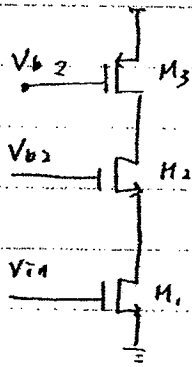
$$sC_1 V_{in} = -sC_2 V_{out}$$

$$\frac{V_{out}}{V_{in}} = -\frac{C_1}{C_2}$$

(ii) At high frequency, C_1, C_2 is like a short circuit

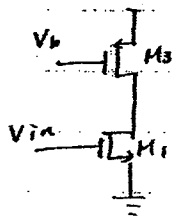
$$\frac{V_{out}}{V_{in}} = 1$$

(b) At low frequency, the equivalent circuit is shown as



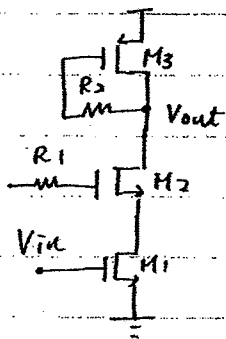
$$A_v \approx -g_{m1} r_{o3} \rightarrow \infty, \text{ if } \lambda = 0$$

(ii) At high frequency, the equivalent circuit

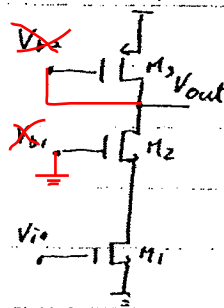


$$A_V = -g_{m1}(r_{o1} // r_{o3}) \rightarrow \infty \text{ if } \lambda = 0$$

(c) (i) At low frequency, the equivalent circuit



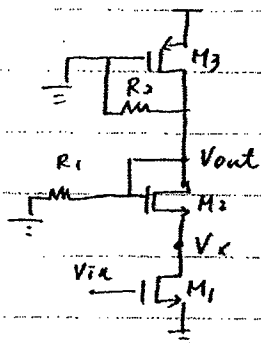
R_1, R_2 can be ignored $\Rightarrow$



The impedance @ $V_{out} = \frac{1}{g_{m3}}$

$$A_V \cong -g_{m1} \cdot \frac{1}{g_{m3}} = -\frac{g_{m1}}{g_{m3}}$$

(ii) At high frequency,



$$\frac{V_X}{V_{in}} = -g_{m1} \cdot \frac{1}{g_{m2}}$$

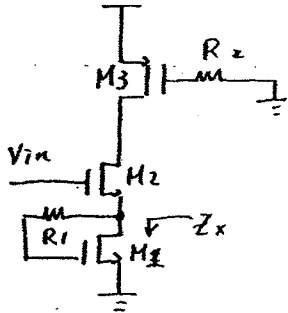
[the impedance looking into V_X

The impedance @ $V_{out} = R_1 // R_2$

$$\therefore A_V = \left(-g_{m1} \cdot \frac{1}{g_{m2}} \right) \cdot g_{m2} \cdot (R_1 // R_2) = -g_{m1} (R_1 // R_2)$$

✱

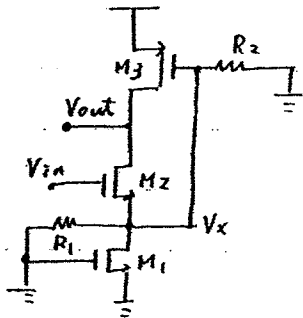
(d) (i) At low frequency, the equivalent circuit is



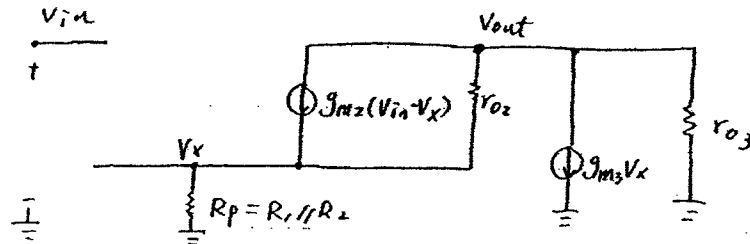
$$\frac{V_{out}}{V_{in}} = \frac{g_{m2}(r_{o2} \parallel (1 + g_{m3}r_{o3})Z_x)}{1 + g_{m2}Z_x} \approx \frac{g_{m2}(r_{o2} \parallel r_{o3})}{1 + \frac{g_{m2}}{g_{m1}}} \rightarrow \infty \text{ if } \lambda = 0$$

$$Z_x = \frac{1}{g_m}$$

(ii) At high frequency



Small-signal model



$$\text{KCL @ } V_X, V_{out} : \frac{V_X}{R_p} = g_{m2}(V_{in} - V_X) + \frac{V_{out} - V_X}{r_{o2}} = -\left(g_{m3}V_X + \frac{V_{out}}{r_{o3}}\right)$$

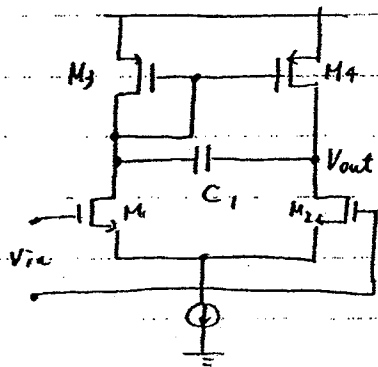
$$\frac{V_X}{R_p} = -\left(g_{m3}V_X + \frac{V_{out}}{r_{o3}}\right) \Rightarrow \frac{V_{out}}{V_X} = -r_{o3}\left(g_{m3} + \frac{1}{R_p}\right)$$

$$g_{m2}(V_{in} - V_X) + \frac{V_{out} - V_X}{r_{o2}} = \frac{V_X}{R_p} \Rightarrow g_{m2}V_{in} = \left(\frac{1}{R_p} + \frac{1}{r_{o2}} + g_{m2}\right)V_X + \frac{V_{out}}{r_{o2}}$$

$$\Rightarrow g_{m2}V_{in} = \left[-\left(\frac{1}{R_p} + \frac{1}{r_{o2}} + g_{m2}\right)\frac{1}{r_{o3}(g_{m3} + \frac{1}{R_p})} + \frac{1}{r_{o2}}\right]V_{out}$$

$$\Rightarrow \frac{V_{out}}{V_{in}} = \frac{-g_{m2}r_{o3}(g_{m3} + \frac{1}{R_p})}{\left(\frac{1}{R_p} + \frac{1}{r_{o2}} + g_{m2}\right) - \frac{r_{o3}}{r_{o2}}(g_{m3} + \frac{1}{R_p})} \rightarrow \infty \text{ if } \lambda = 0$$

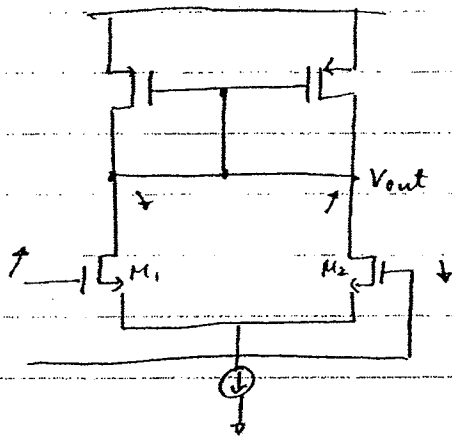
6.10(a) (i) At low frequency



C_1 is like an open circuit @ very low frequency

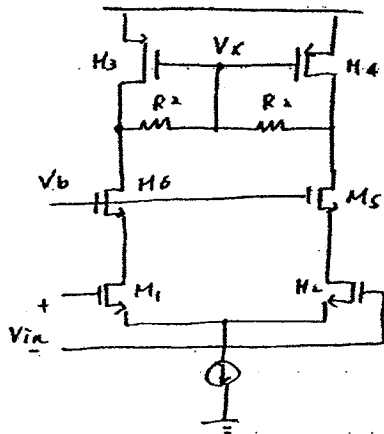
$$\Rightarrow \frac{V_{out}}{V_{in}} = -g_{m1}(r_{o2} \parallel r_{o4}) \rightarrow \infty \text{ if } \lambda = 0$$

(ii) At very high frequency, C_1 is like a short circuit

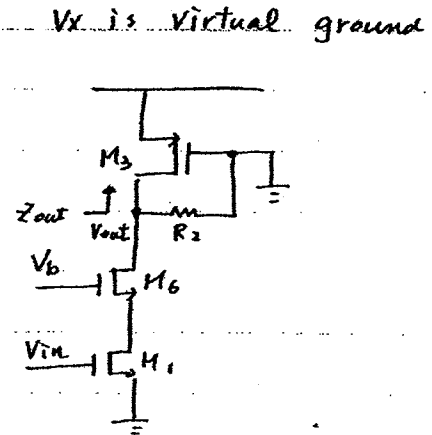


$$\text{Gain} = 0$$

6.10 (b) (i) At low frequency, the equivalent circuit is



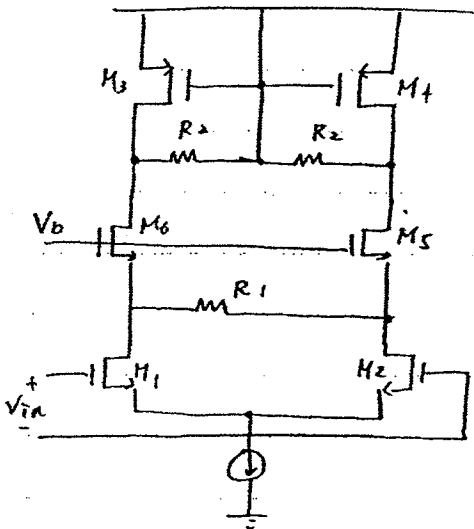
half circuit



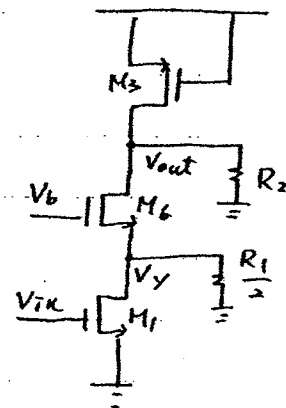
$$Z_{out} \cong r_{o3} \parallel R_2 \cong R_2$$

$$A_v = -g_{m1} \cdot (R_2 \parallel r_{o3}) \cong -g_{m1} R_2$$

(ii) At high frequency



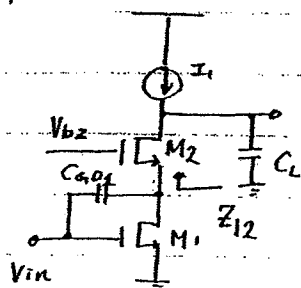
half circuit



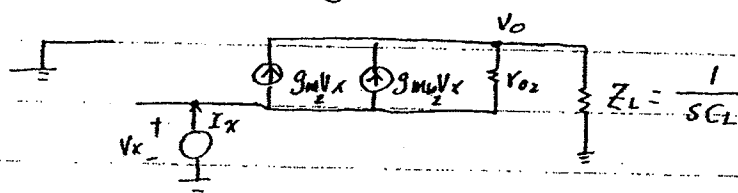
$$\frac{V_y}{V_{in}} = -g_{m1} \left(\frac{1}{g_{m6}} \parallel \frac{R_1}{2} \right), \quad \frac{V_{out}}{V_y} \cong +g_{m6} \cdot R_2$$

$$\frac{V_{out}}{V_{in}} = - \frac{g_{m1} g_{m6} R_1 R_2}{(2 + g_{m6} \cdot R_1)} *$$

6.11



The impedance Z_{12} can be derived from the following small signal model



$$\text{KCL @ } V_o: \frac{V_o}{Z_L} + \frac{V_o - V_x}{r_{o2}} = (g_{m2} + g_{mb2})V_x \Rightarrow \left(\frac{1}{Z_L} + \frac{1}{r_{o2}}\right)V_o = (g_{m2} + g_{mb2} + \frac{1}{r_{o2}})V_x$$

$$\Rightarrow V_o = \left(\frac{g_{m2} + g_{mb2} + \frac{1}{r_{o2}}}{1 + \frac{Z_L}{r_{o2}}}\right)V_x$$

$$\Rightarrow I_x = \frac{V_o}{Z_L} = \left[\frac{g_{m2} + g_{mb2} + \frac{1}{r_{o2}}}{1 + \frac{Z_L}{r_{o2}}}\right]V_x \Rightarrow \frac{V_x}{I_x} = Z_{12} = \frac{1 + \frac{Z_L}{r_{o2}}}{g_{m2} + g_{mb2} + \frac{1}{r_{o2}}}$$

$$\Rightarrow Z_{12} = \frac{r_{o2} + Z_L}{1 + (g_{m2} + g_{mb2})r_{o2}}$$

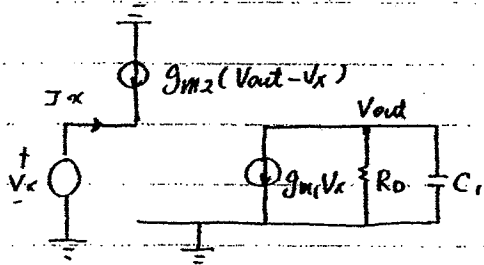
The miller multiplication for $C_{GD1} = 1 + g_{m1}Z_{12}$

$$= 1 + \frac{g_{m1}(r_{o2} + Z_L)}{1 + (g_{m2} + g_{mb2})r_{o2}} \quad \text{--- (1)}$$

If C_L is relatively large $\Rightarrow \left|\frac{1}{sC_L}\right| \ll r_{o2}$

$$\text{eg } \textcircled{1} \text{ can be approximated as } \approx 1 + \frac{g_{m1}r_{o2}}{1 + (g_{m2} + g_{mb2})r_{o2}} \approx 1 + \frac{g_{m1}}{g_{m2} + g_{mb2}}$$

6.12 (a)



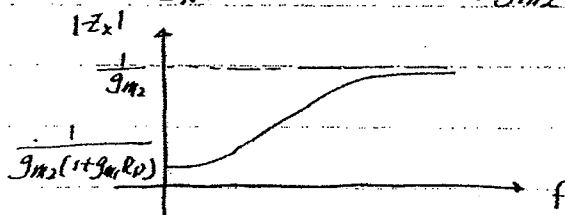
$$V_{out} = -g_{m1}V_x (R_D \parallel \frac{1}{sC_1})$$

$$I_x = -g_{m2}(V_{out} - V_x) = -g_{m2}V_{out} + g_{m2}V_x = [g_{m2}g_{m1}(R_D \parallel \frac{1}{sC_1}) + g_{m2}]V_x$$

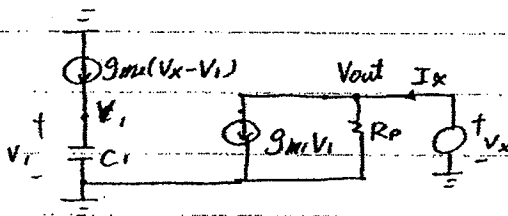
$$Z_x = \frac{V_x}{I_x} = \frac{1}{g_{m2}g_{m1} \frac{R_D \parallel \frac{1}{sC_1}}{R_D + \frac{1}{sC_1}} + g_{m2}} = \frac{1}{g_{m2} \left[\left(\frac{g_{m1}R_D}{1 + sR_DC_1} \right) + 1 \right]}$$

$$\text{Thus, } Z_x(s \rightarrow 0) = \frac{1}{g_{m2}(1 + g_{m1}R_D)}$$

$$Z_x(s \rightarrow \infty) = \frac{1}{g_{m2}}$$



(b)



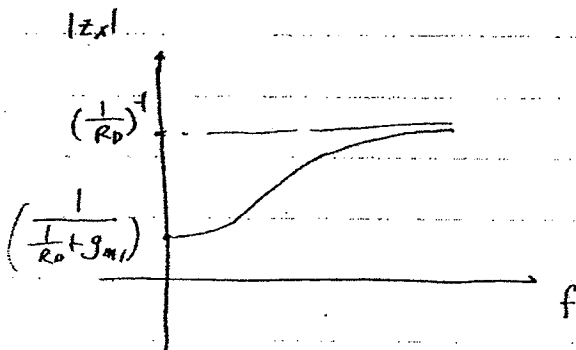
$$\text{KCL @ } V_1: g_{m2}(V_x - V_1) = sC_1 V_1$$

$$\Rightarrow V_1 = \left(\frac{g_{m2}}{sC_1 + g_{m2}} \right) V_x$$

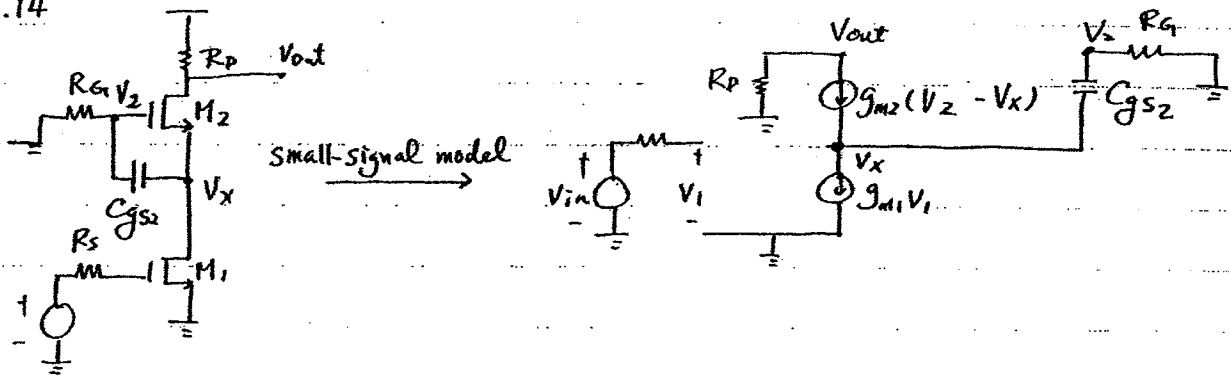
$$\text{KCL @ } V_{out}: I_x = \frac{V_x}{R_D} + g_{m1}V_1$$

$$= \frac{V_x}{R_D} + \frac{g_{m1}g_{m2}}{sC_1 + g_{m2}} V_x$$

$$\Rightarrow Z_x = \frac{1}{\frac{1}{R_D} + \frac{g_{m1}g_{m2}}{sC_1 + g_{m2}}}$$



6.14



$$\text{KCL @ } V_2 : \frac{V_2}{R_{G2}} = sC_{gs2}(V_x - V_2)$$

$$\Rightarrow \frac{V_2}{V_x} = \frac{sC_{gs2}}{\frac{1}{R_{G2}} + sC_{gs2}} = \frac{sR_{G2}C_{gs2}}{1 + sR_{G2}C_{gs2}} \quad \text{--- ①}$$

$$\text{KCL @ } V_{out} : V_{out} = -g_{m2}(V_2 - V_x)R_D = \left[\frac{g_{m2}R_D}{1 + sR_{G2}C_{gs2}} \right] V_x \quad \text{--- ②}$$

$$\text{KCL @ } V_x : g_{m1}V_1 = g_{m1}V_{in} = (g_{m2} + sC_{gs2})(V_2 - V_x)$$

$$= \frac{-(g_{m2} + sC_{gs2})}{1 + sR_{G2}C_{gs2}} V_x \quad \text{--- ③}$$

$$\text{from ①, ②, } \frac{V_{out}}{V_{in}} = \frac{-g_{m1}g_{m2}R_D}{g_{m2} + sC_{gs2}} \quad *$$

Problem 9.7

Design the op amp of fig. 9.21

Max diff. swing = 4V

 total Power = 6mW $I_{SS} = 0.5\text{mA}$

 Total current driven by $V_{DD} = \frac{6\text{mW}}{3\text{V}} = 2\text{mA}$

$$I_{D5} + I_{D6} = 2\text{mA} - I_{SS} = 1.5\text{mA} \Rightarrow I_{D5} = I_{D6} = 0.75\text{mA}$$

$$\text{Max diff swing} = 2[V_{DD} - |V_{D05}| - V_{D07}] = 4\text{V}$$

$$\Rightarrow |V_{D05}| + |V_{D07}| = 1 \quad \text{choose } V_{D05} = 0.6\text{V}, \quad V_{D07} = 0.4\text{V}$$

$$I_D = \frac{1}{2} \mu C_{ox} \left(\frac{W}{L} \right)_{\text{eff}} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$$

$$\left(\frac{W}{L} \right)_{\text{eff}5} = \frac{2I_D}{\mu_p C_{ox} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})} = \frac{2(0.75\text{mA})}{(100)(383.6 \times 10^{-9})(0.6)^2 (1 + 0.2 \times 0.6)}$$

$$\left(\frac{W}{L} \right)_{\text{eff}5} = 97 \Rightarrow W_{5,6} = 97 \times 0.32\mu\text{m} = 31\mu\text{m}$$

$$\left(\frac{W}{L} \right)_{\text{eff}7} = \frac{2(0.75\text{mA})}{(350)(383.6 \times 10^{-9})(0.4)^2 (1 + 0.1(0.4))}$$

$$= 67 \Rightarrow W_{7,8} = 67 \times 0.34\mu\text{m} = 23\mu\text{m}$$

 We are generally not worried about the swing of let stage, assume $|V_{D03}| = 1\text{V}$, $V_{D01} = 1\text{V}$.

$$\left(\frac{W}{L} \right)_{\text{eff}3} = \frac{2(0.25\text{mA})}{(100)(383.6 \times 10^{-9})(1)^2 (1 + 0.2(1))} = 10.86$$

$$W_{3,4} = 3.5\mu\text{m}$$

$$\left(\frac{W}{L} \right)_{\text{eff}1} = \frac{2(0.25\text{mA})}{(350)(383.6 \times 10^{-9})(1)^2 (1 + 0.1)} = 3.4$$

$$W_{1,2} = 1.2\mu\text{m}$$

$$V_{b1} = V_{DD} - |V_{D03}| - V_{TH3} = 3 - 1 - 0.8 = 1.2\text{V}$$

$$V_{in,CM} = V_{ISS} + V_{TH1} + V_{D01} = 0.3 + 0.7 + 1.0 = 2\text{V}$$

$$V_{b2} = V_{TH7} + V_{D07} = 0.7 + 0.4 = 1.1\text{V}$$

 Summary $L = 0.5\mu\text{m}$

$$W_{1,2} = 1.2\mu\text{m}$$

$$V_{b1} = 1.2\text{V}$$

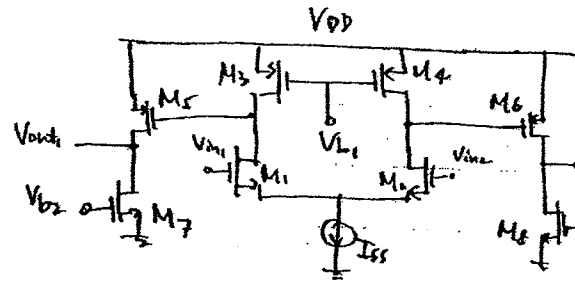
$$W_{3,4} = 3.5\mu\text{m}$$

$$V_{b2} = 1.1\text{V}$$

$$W_{5,6} = 31\mu\text{m}$$

$$V_{in,CM} = 2\text{V}$$

$$W_{7,8} = 23\mu\text{m}$$



Problem 9.18

$P = 6mW$, output swing = 2.5V

$L_{eff} = 0.5\mu m$

$$a) I_{D5} = 1mA. V_{D5} \approx V_{D6} = \frac{V_{DD} - \text{Output Swing}}{2} = \frac{3 - 2.5}{2} = 0.25V$$

$$I_D = \frac{1}{2} \mu C_{ox} \left(\frac{W}{L}\right) (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$$

$$\left(\frac{W}{L}\right)_{eff} = \frac{2I_D}{\mu C_{ox} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})}$$

$$\left(\frac{W}{L}\right)_5 = \frac{2(1mA)}{(350)(383.6n)(0.25)^2(1 + 0.1)(0.25)} = 233$$

$$I_{D5} = I_{D6} = 1mA$$

$$\left(\frac{W}{L}\right)_6 = \frac{2(1mA)}{(100)(383.6n)(0.25)^2(1 + 0.2)(0.25)} = 795$$

$$\boxed{\left(\frac{W}{L}\right)_5 = 233 \quad \left(\frac{W}{L}\right)_6 = 795}$$

$$b, A_v \text{ of 1st stage} = g_{m5} (r_{o2} \parallel r_{o4})$$

$$A_v \text{ of 2nd stage} = g_{m5} (r_{o5} \parallel r_{o6})$$

$$g_{m5} = \frac{2I_D}{V_{GS} - V_{TH}} = \frac{2(1mA)}{0.25} = 8mS$$

$$r_{o5} = \frac{1}{\lambda I_D} = \frac{1}{(0.1)(1mA)} = 10k\Omega$$

$$r_{o6} = \frac{1}{\lambda I_D} = \frac{1}{(0.2)(1mA)} = 5k\Omega$$

$$\boxed{A_v \text{ of output stage} = (8m)(10k \parallel 5k) = 26.67}$$

$$c1) I_{D1} = 1mA \rightarrow I_{D3} = I_{D4} = 0.5mA$$

$$V_{GS5} - V_{TH} = 0.25V \Rightarrow V_{GS5} = 0.25 + V_{TH} = 0.95V$$

$$V_{GS3} - V_{TH} = 0.25$$

$$\left(\frac{W}{L}\right)_{3,4} = \frac{2(0.5mA)}{(350)(383.6n)(0.25)^2(1 + 0.1)(0.25)}$$

$$\boxed{\left(\frac{W}{L}\right)_{3,4} = 116}$$

9.18

$$d) A_{v_{tot}} = g_{m1}(r_{o2} \parallel r_{o4}) g_{m5}(r_{o5} \parallel r_{o6})$$

$$r_{o2} = \frac{1}{\lambda I_0} = \frac{1}{(0.2)(0.5\text{mA})} = 10\text{k}\Omega$$

$$r_{o4} = \frac{1}{(0.1)(0.5\text{mA})} = 20\text{k}\Omega$$

$$r_{o2} \parallel r_{o4} = 6.67\text{k}\Omega$$

$$A_{v_{tot}} = g_{m1}(6.67\text{k})(26.7) = 500$$

$$g_{m1} = 2.81\text{mA/V}$$

$$g_{m1} = \sqrt{2\mu_n C_{ox} \left(\frac{W}{L}\right) I_0} \Rightarrow \left(\frac{W}{L}\right) = \frac{g_{m1}^2}{2\mu_n C_{ox} I_0}$$

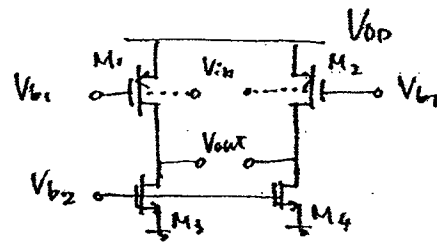
$$\left(\frac{W}{L}\right)_{1,2} = \frac{(2.81\text{mA/V})^2}{2(100)(383.6\text{n})(0.5\text{mA})}$$

$$\boxed{\left(\frac{W}{L}\right)_{1,2} = 206}$$

9.22.

(a) $A_v = g_{m_{b1,2}} (r_{o1} \parallel r_{o3})$

b, $V_{in} > V_{DD} - V_{D1}$ where V_{D1} is the diode junction voltage of the diode between source and body.



(c) $g_{mb} = g_m \frac{\gamma}{2\sqrt{|\phi_F| + |V_{SB}|}}$

As $V_{in,cm}$ decreases, $|V_{SB}| \uparrow$, g_{mb} decreases.

More accurately, $g_{mb} \propto \frac{1}{\sqrt{|\phi_F| + |V_{SB}|}}$

As a result, A_v decreases.

(d)

$$\begin{aligned} \overline{V_{n,out}^2} &= [4kT\gamma (g_{m1} + g_{m3}) R_{out}]^2 \times 2 \\ \overline{V_{n,in}^2} &= \frac{4kT\gamma (g_{m1} + g_{m3}) R_{out} \times 2}{[g_{m_{b1,2}} (R_{out})]^2} \\ &= \left[4kT\gamma \frac{g_{m1} + g_{m3}}{(g_{m_{b1,2}})^2} \right] \times 2 \end{aligned}$$

Problem 9.23.

a. Av of 1st stage = $g_{m1,2} (r_{o1} // r_{o3})$

Av of 2nd stage = $[g_{m5,9} (r_{o7} // r_{o5})] \times 2$

Av-tot = $g_{m1,2} (r_{o1} // r_{o3}) g_{m5,9} (r_{o5} // r_{o7}) \times 2$

b. 1st major pole:

$$\omega_1 = \frac{1}{(r_{o1} // r_{o3}) [C_{DG9} + C_{DB9} + C_{GS11} + C_{DB11} + C_{GS7} + C_{GD7} (1 + g_{m7} (r_{o5} // r_{o7}))]}$$

2nd major pole: node X, Y

$$\omega_X = \frac{1}{(r_{o1} // r_{o3}) \left[C_{DE1} + C_{DB1} + C_{DG3} + C_{DB3} + C_{GS10} + C_{GD10} \left(1 + \frac{g_{m10}}{g_{m12}} \right) + C_{GS5} + C_{GD5} (1 + g_{m5} (r_{o5} // r_{o7})) \right]}$$

3rd major pole: node output

$$\omega_{out} = \frac{1}{(r_{o5} // r_{o7}) (C_{GD5} + C_{DB5} + C_{GD7} + C_{DB7})}$$

Prob. 9.24.

Av of fast path: $g_{m1}' (r_{o5} // r_{o7})$

Av of slow path: $g_{m1} (r_{o1} // r_{o3}) g_{m5} (r_{o5} // r_{o7})$

Overall gain Av-tot = $\left[\frac{g_{m1}' + g_{m1} g_{m5} (r_{o1} // r_{o3})}{2} \right] (r_{o5} // r_{o7})$

The output swing is usually limited by M5-8, i.e.

$$V_{OD} - |V_{OD7}| - V_{OD5}$$