

Chapter 2:

$$m_0 v = \frac{\hbar}{\lambda} \equiv \hbar k$$

$$\frac{d^2\psi}{dx^2} + \frac{2m_0}{\hbar^2} [E - U] \psi(x) = 0$$

$$\frac{d^2\psi}{dx^2} + g^2 \psi(x) = 0$$

Gen. solutions ($U = \text{constant}$):

$$\psi(x) = A \sin(gx) + B \cos(gx)$$

$$\text{or: } \psi(x) = A \exp(igx) + B \exp(-igx)$$

Bloch's Theorem: $\psi(x+a) = e^{ika} \psi(x)$

$$k = \frac{2\pi n}{Na}, \quad (n = 0, \pm 1, \pm 2, \dots \pm N/2)$$

Chapter 3:

$$v = \frac{1}{\hbar} \frac{dE}{dk}$$

$$m^* = \left[\frac{1}{\hbar^2} \frac{d^2E}{dk^2} \right]^{-1}$$

$$\vec{J} = \frac{1}{\Omega} \sum_{\text{filled states}} -qv_k$$

Chapter 4:

$$n_i = p_i$$

$$n_0 p_0 = n_i^2$$

$$g_C(E) = \frac{8\sqrt{2}\pi}{h^3} m_e^{*3/2} (E - E_C)^{1/2}$$

$$f(E) = \frac{1}{1 + \exp[(E - E_F)/kT]}$$

$$N_C = 2 \left(\frac{2\pi m_e^* kT}{h^2} \right)^{3/2}$$

$$n_0 = N_C \exp \left(\frac{E_F - E_C}{kT} \right)$$

$$p_0 = N_V \exp \left(\frac{E_V - E_F}{kT} \right)$$

$$f_{MB}(E) = e^{-\frac{(E-E_F)}{kT}}$$

$$n_i = N_C \exp \left(\frac{E_{Fi} - E_C}{kT} \right)$$

$$p_i = N_V \exp \left(\frac{E_V - E_{Fi}}{kT} \right)$$

$$\int_{\text{device}} q(p(x) - n(x) + N_D(x) - N_A(x)) dx = 0$$

$$n_0 = n_i \exp \left(\frac{E_F - E_{Fi}}{kT} \right)$$

$$p_0 = n_i \exp \left(\frac{E_{Fi} - E_F}{kT} \right)$$

Chapter 5:

$$v_R = \sqrt{\frac{kT}{2\pi m^*}}$$

$$1/v_d = 1/\mu \mathcal{E} + 1/v_{\text{sat}}$$

$$\mu \equiv \frac{q\tau_{\text{coll}}}{m^*}$$

$$\vec{J}_{e,\text{drift}} = -qn\vec{v}_d = -qn\mu_e(-\vec{\mathcal{E}})$$

$$\vec{J}_{h,\text{drift}} = qp\vec{v}_d = qp\mu_e \vec{\mathcal{E}}$$

$$\sigma = 1/\rho = q(n\mu_e + p\mu_h)$$

$$\vec{J}_{h,\text{diff}} = -qD_h \frac{dp}{dx}$$

$$\vec{J}_{e,\text{diff}} = qD_e \frac{dn}{dx}$$

$$D_e = \frac{kT}{q} \mu_e$$

$$\frac{\partial n}{\partial t} = \frac{1}{q} \frac{dJ_e}{dx} - \frac{n - n_0}{\tau_e}$$

$$\frac{\partial p}{\partial t} = -\frac{1}{q} \frac{dJ_h}{dx} - \frac{p - p_0}{\tau_h}$$

Gen. solution to Cont. Eqns.:

$$c(x) - c_0 = A \exp(-x/\sqrt{D_e \tau_e}) + B \exp(x/\sqrt{D_e \tau_e})$$

Chapter 6:

$$-q\psi(x) = E_l(x) - E_0$$

$$V_{bi} = \frac{kT}{q} \ln \left[\frac{N_D N_A}{n_i^2} \right]$$

$$\psi(-x_N) - \psi(x_P) = V_{bi} + V_a$$

$$E_F(-x_N) - E_F(x_P) = -qV_a$$

$$W = \sqrt{\frac{2e}{q} (V_{bi} + V_a) \left(\frac{1}{N_D} + \frac{1}{N_A} \right)}$$

$$n = n_i \exp \left(\frac{E_{Fn} - E_{Fi}}{kT} \right)$$

$$p = n_i \exp \left(\frac{E_{Fi} - E_{Fp}}{kT} \right)$$

$$-q\phi_n(x) = E_{Fn}(x) - E_F$$

$$-q\phi_p(x) = E_{Fp}(x) - E_F$$

$$\vec{J}_T = \vec{J}_e + \vec{J}_h = -q\mu_e n \nabla \phi_n - q\mu_h p \nabla \phi_p$$

$$-\nabla^2 \psi = \frac{q}{\epsilon} [p - n + N_D - N_A]$$

$$J_e = -qn\mu_e \nabla \psi + qD_e \nabla n$$

$$J_h = -qp\mu_h \nabla \psi - qD_h \nabla p$$

$$\frac{\partial n}{\partial t} = \frac{1}{q} \nabla \cdot J_e - \frac{n - n_0}{\tau_e}$$

$$\frac{\partial p}{\partial t} = -\frac{1}{q} \nabla \cdot J_h - \frac{p - p_0}{\tau_h}$$

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$$n(x_{dp}) = n_{0p} \exp \left(\frac{-qV_{ai}}{kT} \right)$$

Chapter 7:

$$\partial V_{aj} = \partial V_{GS} \frac{1}{1 + C_S/C_{ox}}$$

$$V_{bi} = \frac{\Phi_S - \Phi_G}{q} = -V_{fb}$$

$$-qV_{CB}(x) = E_{Fn}(x) - E_{FB}$$

$$\psi_s(x) = \frac{2kT}{q} \ln \frac{N_A}{n_i} + V_{CB}(x) \equiv 2\phi_B + V_{CB}(x)$$

$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}}$$

$$Q_B(x) = -\sqrt{2\epsilon_S q N_A (2\phi_B + V_{SB} + V_{CS}(x))}$$

$$V_T = V_{fb} + 2\phi_B + \frac{1}{C_{ox}} \sqrt{2\epsilon_S q N_A (2\phi_B + V_{SB})}$$

$$Q_n(x) = -C_{ox} [V_{GS} - V_{fb} - 2\phi_B - V_{CS}(x) ...]$$

$$... - \frac{1}{C_{ox}} \sqrt{2\epsilon_S q N_A (2\phi_B + V_{SB} + V_{CS}(x))}]$$

$$Q_n(x) \approx -C_{ox} [V_{GS} - V_T - mV_{CS}(x)]$$

$$m = (1 + C_B(0)/C_{ox})$$

$$I_D(\text{LEVEL1}) = ZC_{ox} \left[V_{GS} - V_T - m \frac{V_{DS}}{2} \right] \mu_{\text{eff}} \frac{V_{DS}}{L}$$

$$V_{DSsat} = (V_{GS} - V_T)/m$$

$$1/v_d = 1/\mu \mathcal{E} + 1/v_{\text{sat}}$$

$$I_D(\text{LEVEL49}) = ZC_{ox} \left[V_{GS} - V_T - m \frac{V_{DS}}{2} \right] \dots$$

$$\dots \mu_{\text{eff}} \frac{V_{DS}}{L + (\mu_{\text{eff}} V_{DS}/v_{\text{sat}})}$$

$$V_{DSsat} = \frac{2(V_{GS} - V_T)/m}{\sqrt{1 + 2\mu_{\text{eff}}(V_{GS} - V_T)/(mv_{\text{sat}}L) + 1}}$$

Chapter 8:

$$L_e = \sqrt{D_e \tau_e}$$

$$n_E^* = n_{0E} e^{-q(V_{biE} - V_{BE})/kT} = n_{0B} e^{qV_{BE}/kT}$$

$$n(x_{dp}) = n_E^* + \frac{J_e(x_{dp})}{q^2 v_R}$$

$$J_e = -qn_{0B} \left[e^{qV_{BE}/kT} - e^{qV_{BC}/kT} \right] \frac{1}{\frac{W_B}{D_e} + \frac{1}{v_R}}$$

$$I_{B,\text{rec}} = Aqn_{0B} \left[(e^{qV_{BE}/kT} - 1) + (e^{qV_{BC}/kT} - 1) \right] \frac{W_B}{2\tau_e}$$

$$I_{B,\text{inj}} = Aqp_{0E} \left[e^{qV_{BE}/kT} - 1 \right] \frac{1}{\frac{T_h}{D_h} + \frac{1}{2v_R}}$$

$$\beta_0 = I_C/I_B$$

$$\alpha_0 = I_C/|I_E|$$

Chapter 9:

$$C_{jk} = -\frac{\partial Q_j}{\partial V_k} (+ \text{ if } k = j)$$

$$C_{jj} = \sum_{k \neq j} C_{jk} = \sum_{k \neq j} C_{kj}$$

$$C'_{EB,j} = \frac{\epsilon_S A_E}{W}$$

$$C'_{EB,b} = q^2 \frac{W_B A_E}{2kT} n_{0p} e^{qV_{BE}/kT}$$

$$C'_{BE,t} = g_m d / (2v)$$

$$C'_{CB} = \frac{\epsilon_S A_C}{d}$$

Chapter 10:

$$E - E_C = \frac{\hbar^2 k_1^2}{2m_1^*} + \frac{\hbar^2 k_2^2}{2m_2^*} + \frac{\hbar^2 k_3^2}{2m_3^*}$$

$$T \approx \exp \left\{ \frac{-4\pi}{h} \int_0^{t_{ox}} \sqrt{2m [U(x) - E]} dx \right\}$$

$$I_{D,\text{sub-threshold}} = ZC_{ox}(m-1) \frac{kT}{q} \dots$$

$$\dots e^{q(V_{GS} - V_T)/mkT} \cdot \left(\frac{\mu_{\text{eff}} kT}{qL} \right)$$

$$S = \left(\frac{\partial \log_{10} I_D}{\partial V_{GS}} \right)^{-1} = 2.303 m \frac{kT}{q}$$

$$m = 1 + \frac{t_{ox} \epsilon_s}{\epsilon_{ox}} \sqrt{\frac{q^2 N_A}{4\epsilon_s kT} \ln(n_i/N_A)}$$

$$\tau = \frac{kV_{DD}C_X}{I_{Dsat}}$$

$$P_{\text{dyn}} = C_X V_{DD}^2 f$$

Chapter 11:

$$i_c = g_m v_{be} + g_o v_{ce}$$

$$i_b = g_\pi v_{be} + g_{12} v_{ce}$$

$$R_{B,\text{spread}} = R_{\text{Bulk}}/3$$

$$2\pi f_T = \frac{g_m}{C_\pi + C_\mu (1 + gmR_{ec})}$$

$$2\pi f_T = \frac{g_m}{C_{gs} + C_{gd} (1 + gmR_{sd})}$$

$$f_{\max} = \sqrt{\frac{f_T}{8\pi R_B C_\mu}}$$

Chapter 12:

$$J_{\text{Schottky}} = qN_C e^{-\phi_B/kT} v_R (e^{-qV_a/kT} - 1)$$

$$\Phi_B = \Phi_G - \chi_S$$

$$I_{D,\text{MESFET}} \propto G_0$$

$$G_0 = qZ\mu N_D a/L$$

$$g_{C,2D,p} = m^*/(\pi \hbar^2)$$

$$n_{2D,p} = \frac{m^* kT}{\pi \hbar^2} \ln \left[e^{(E_F - E_p)/kT} + 1 \right]$$

Chapter 13:

$$S = \overline{v_{n^2}}/\Delta f \text{ or } \overline{i_{n^2}}/\Delta f$$

$$S_{\text{thermal}} = 4kTR$$

$$S_{\text{shot}} = 2qI_{DC}$$

$$S_{1/f} \propto I_{DC}/f$$

$$NF = 10 \log_{10} [N_{\text{out}}/(GN_{\text{in}})]$$

Chapter 14:

$$V_{\text{br}} = \mathcal{E}_{\text{br}}^2 \frac{\epsilon}{2q} \left(\frac{1}{N_D} + \frac{1}{N_A} \right)$$